

# Pulsed TeV Emission from Pulsars in the Synchro-Curvature/IC Framework

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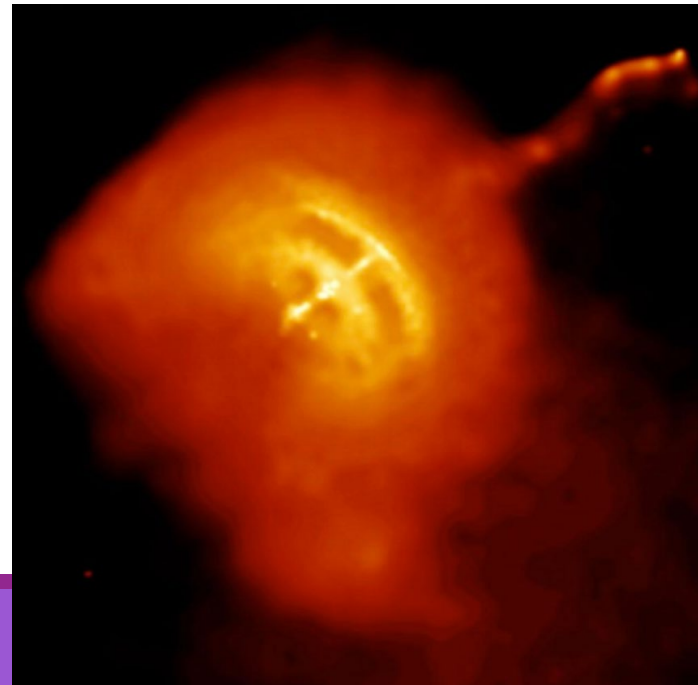
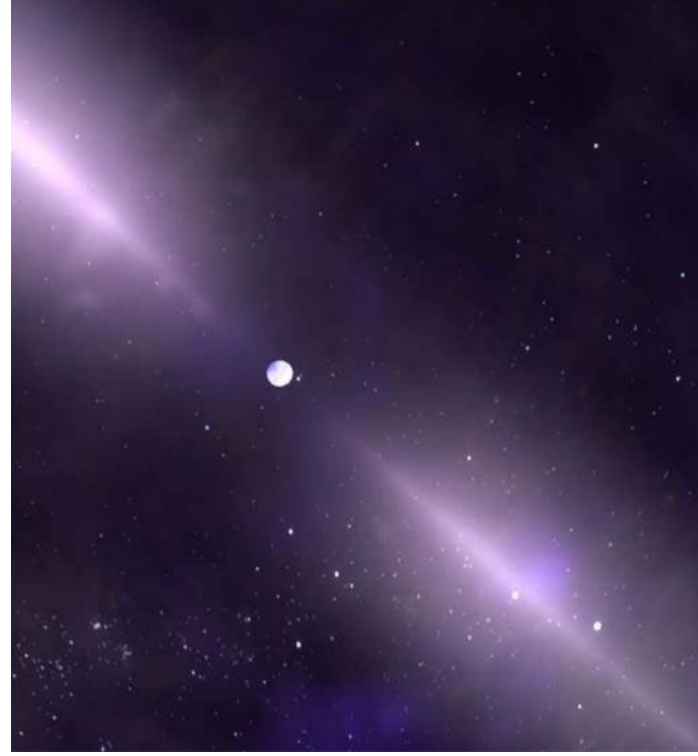
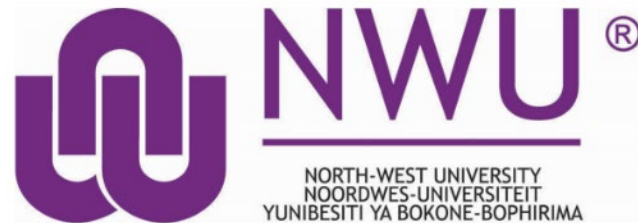
Alice Harding<sup>2</sup>

Constantinos Kalapotharakos<sup>3</sup>

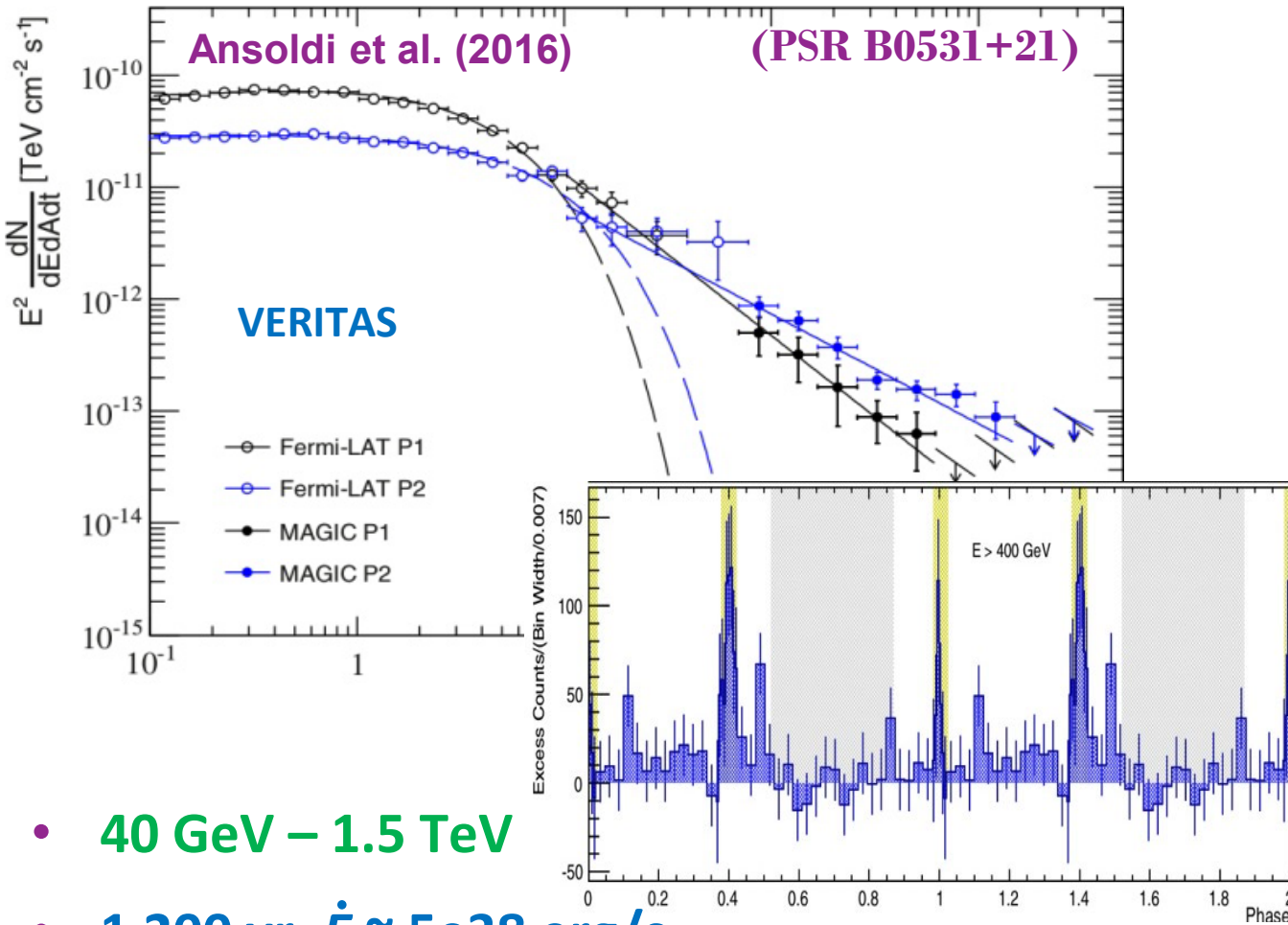
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<sup>2</sup>Los Alamos National Laboratory

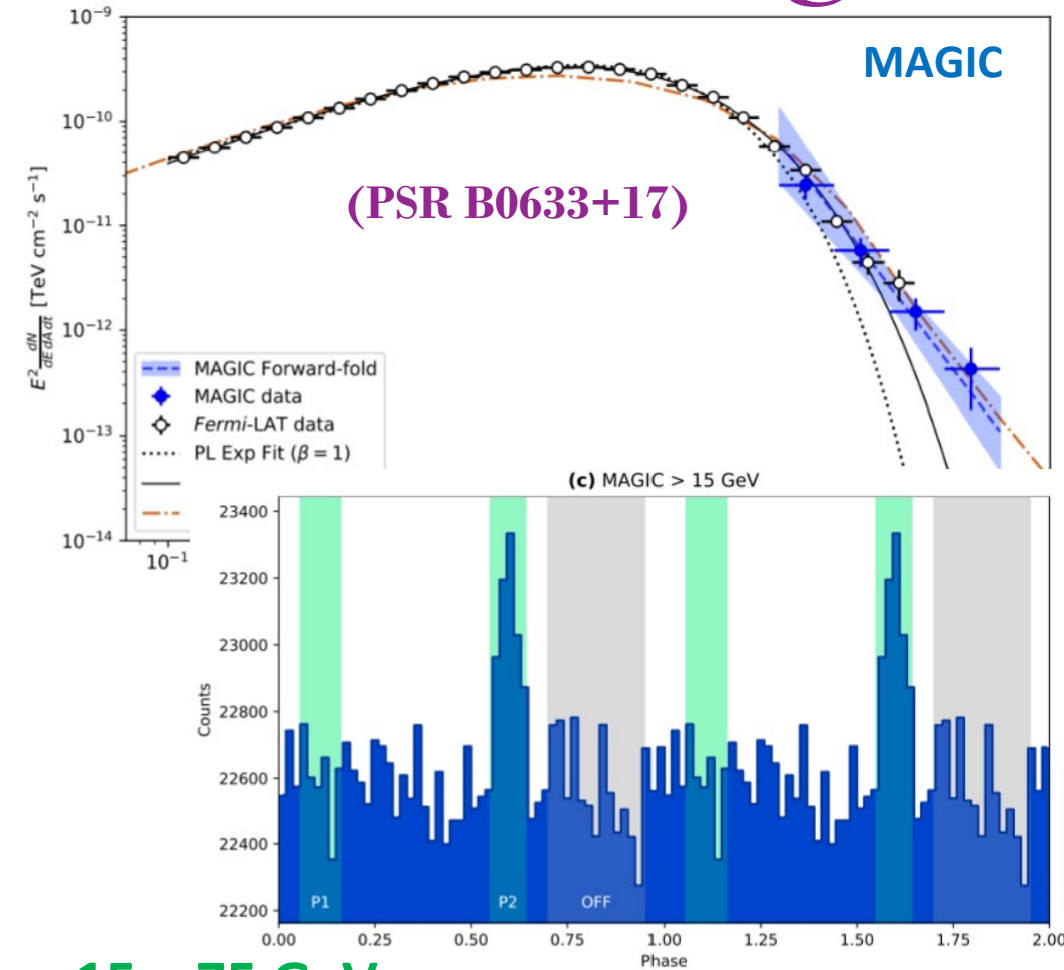
<sup>3</sup>Gravitational Astrophysics Laboratory, NASA/Goddard Space Flight Center



# Pulsed TeV $\gamma$ s from Crab / Geminga

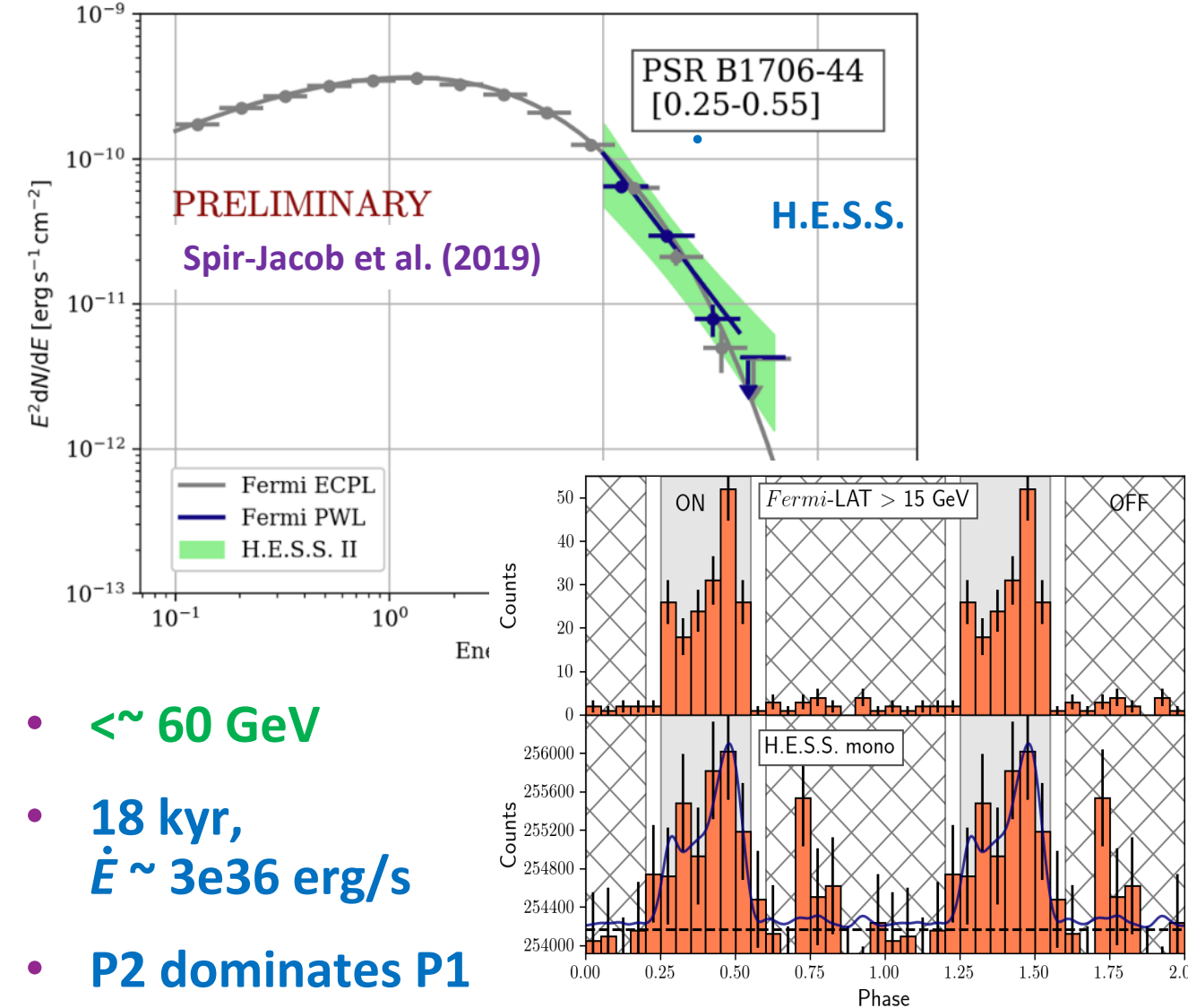


- 40 GeV – 1.5 TeV
- 1 200 yr,  $\dot{E} \sim 5e38 \text{ erg/s}$
- Both P1 and P2 visible

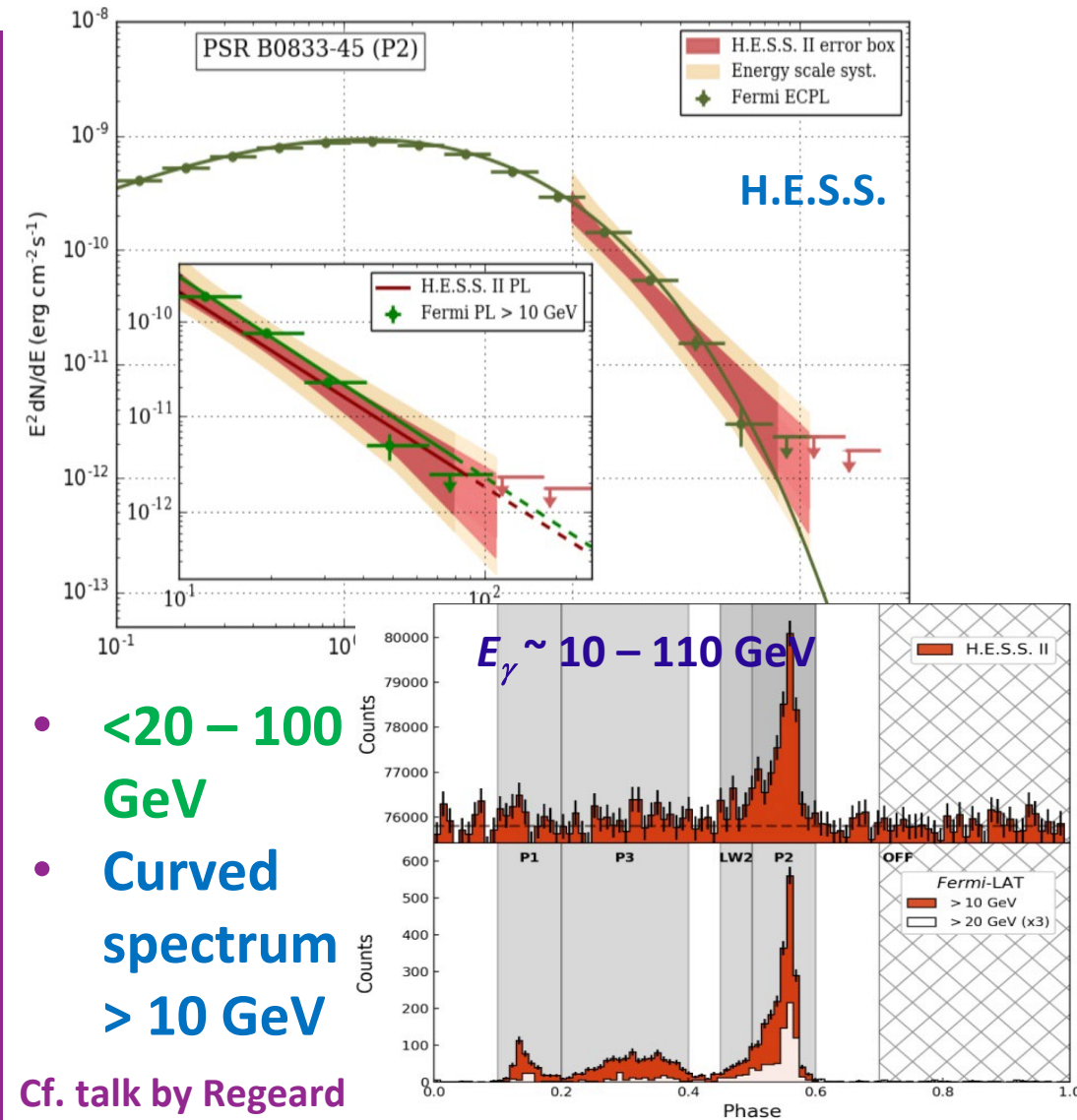


- 15 – 75 GeV
- 340 kyr,  $\dot{E} \sim 3e34 \text{ erg/s}$ ; P2 @  $6.3\sigma$

# Pulsed $\gamma$ s from B1706-44 / Vela



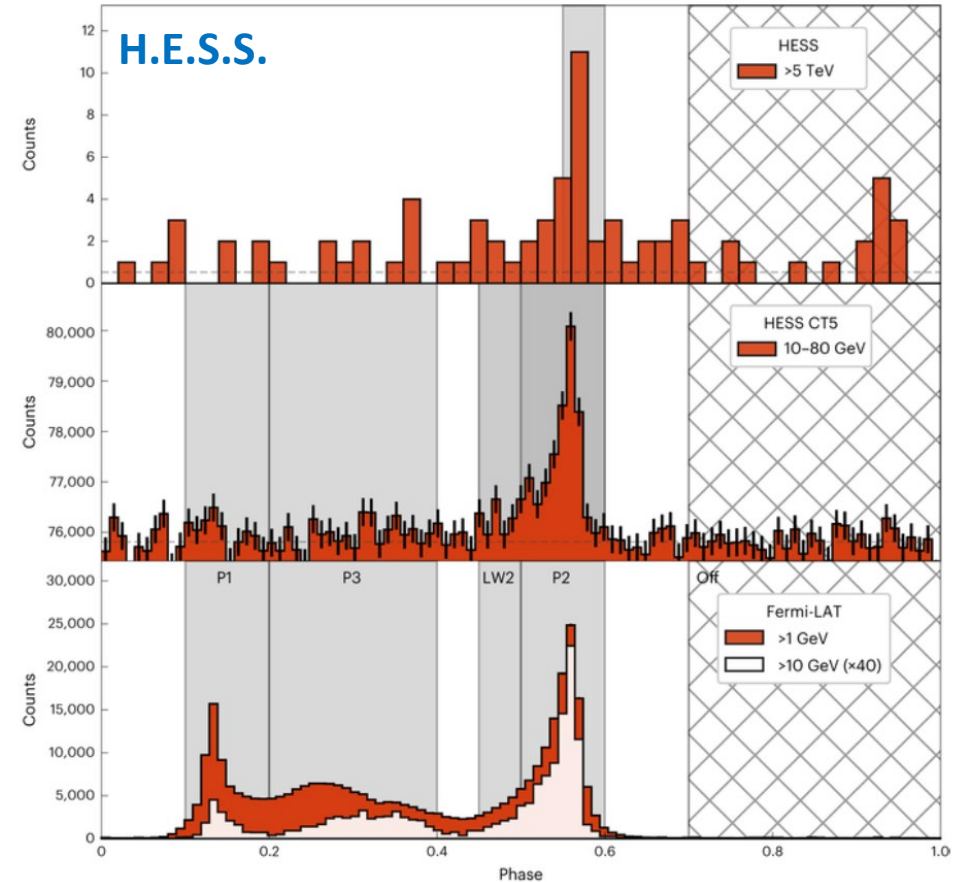
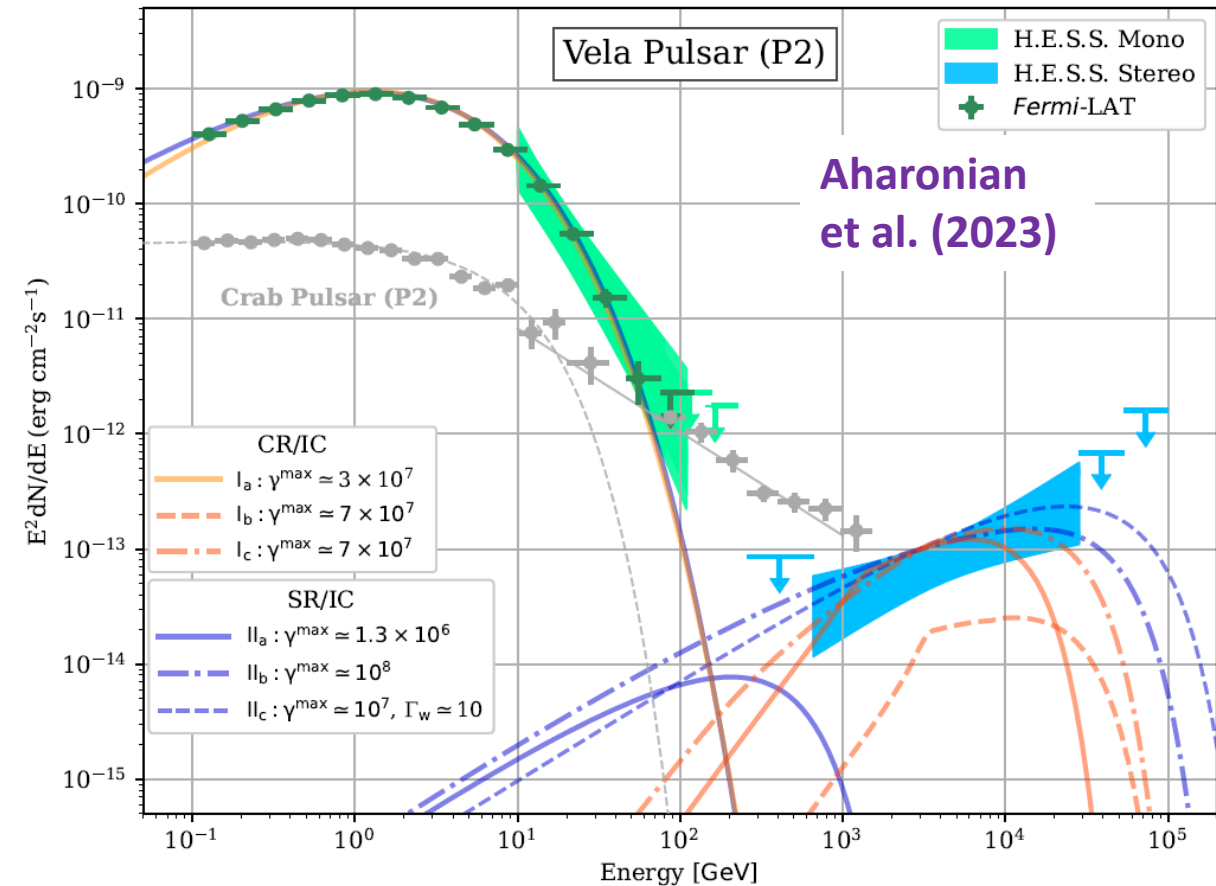
- $< \sim 60$  GeV
- 18 kyr,  
 $\dot{E} \sim 3e36$  erg/s
- P2 dominates P1



- $< 20 - 100$  GeV
- Curved spectrum  
 $> 10$  GeV

Cf. talk by Regnard

# Vela Pulsations $\sim 20$ TeV!



- **New spectral component**
- **Hard index**

Cf. talks by de Ona Wilhelmi, Regard, Djannati-Ataï, etc.

- **P2 remains**
- **Similar P2 peak position & width in HE / VHE**

# Vela Pulsations $\sim 20$ TeV!

## MAIN MODEL FRAMEWORKS:

### (i) Local Models:

Gap models (PC / OG / SG / TPC) within the light cylinder

### (ii) Global Models:

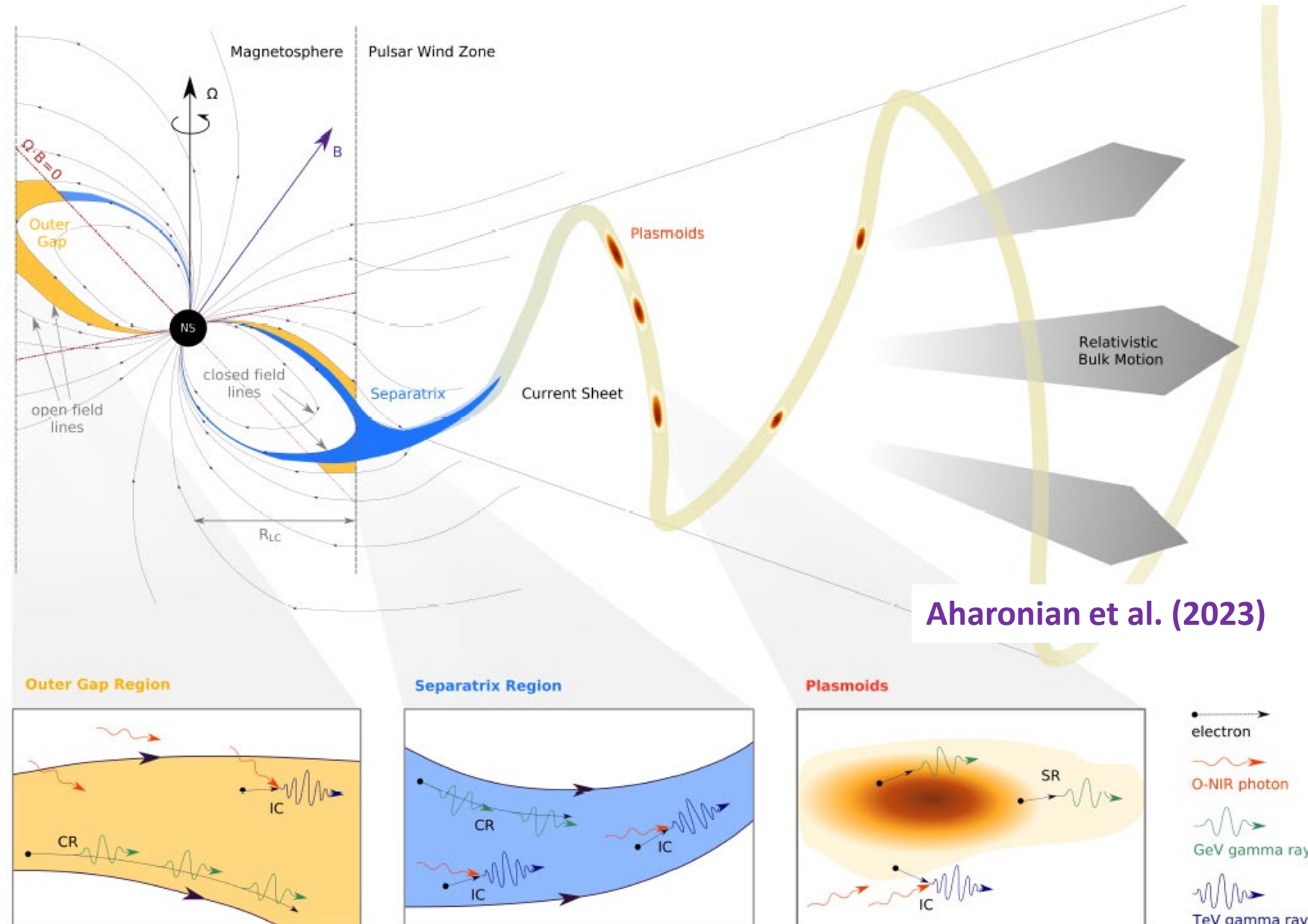
- Separatrix / current sheet model:  $E_{\parallel}$ , SC / IC

- Magnetic reconnection in current sheet; Doppler boosting SR, / IC (striped wind)

Similar caustics than before

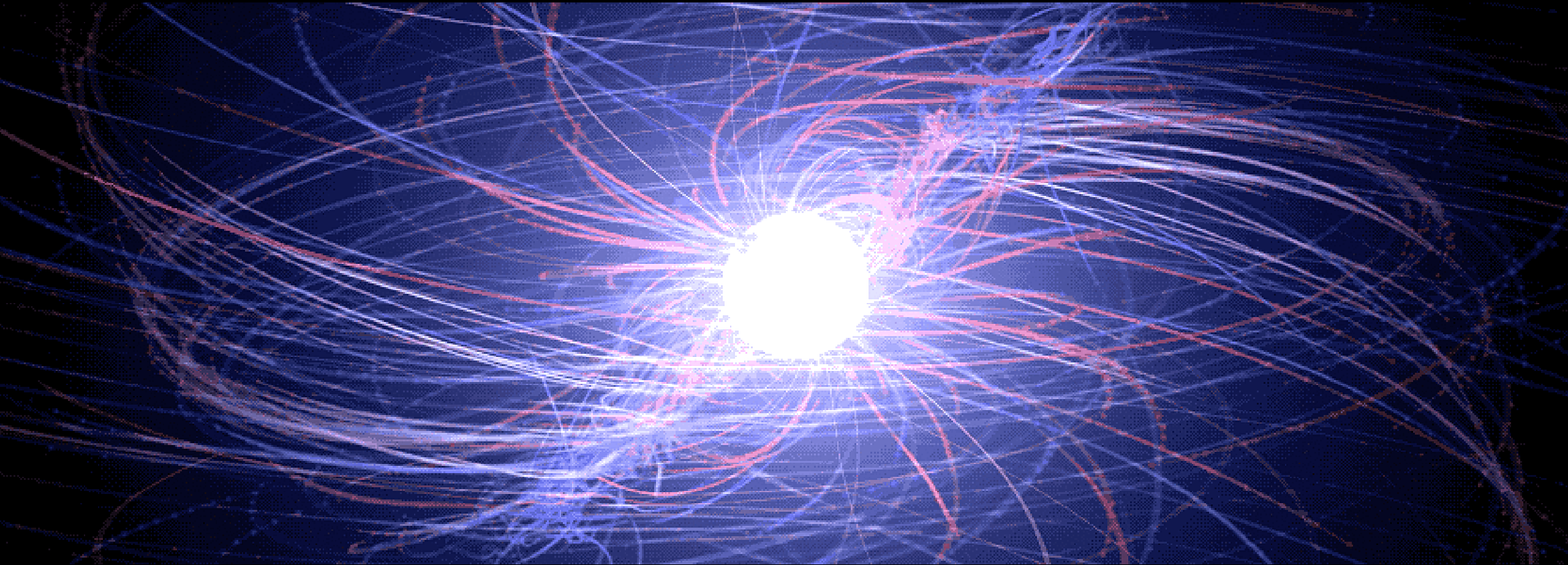
Cf. talks by Pétri, Khangulyan, Philippov, Cerutti, etc.

*HONEST3: The High End of the*



# Model Expectations

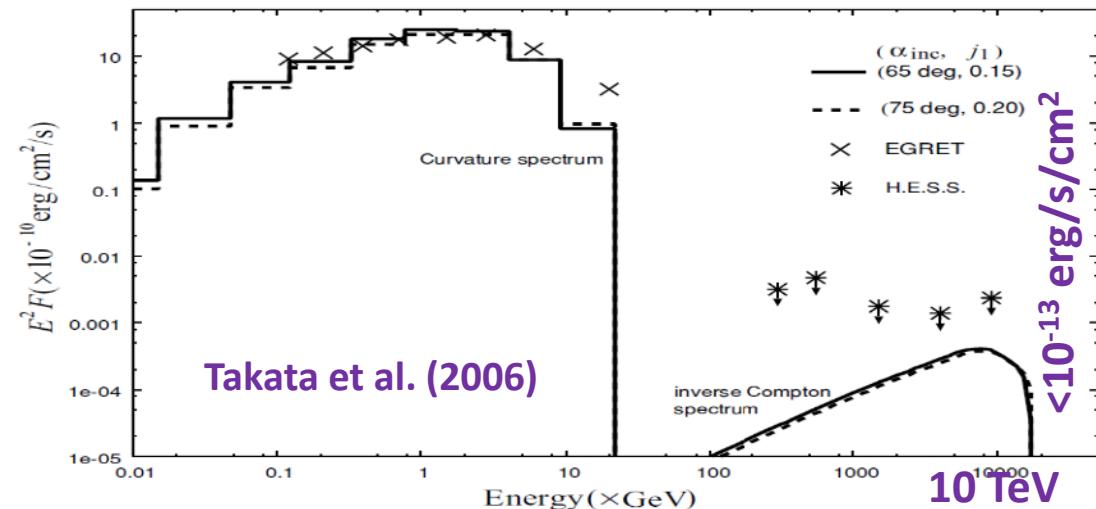
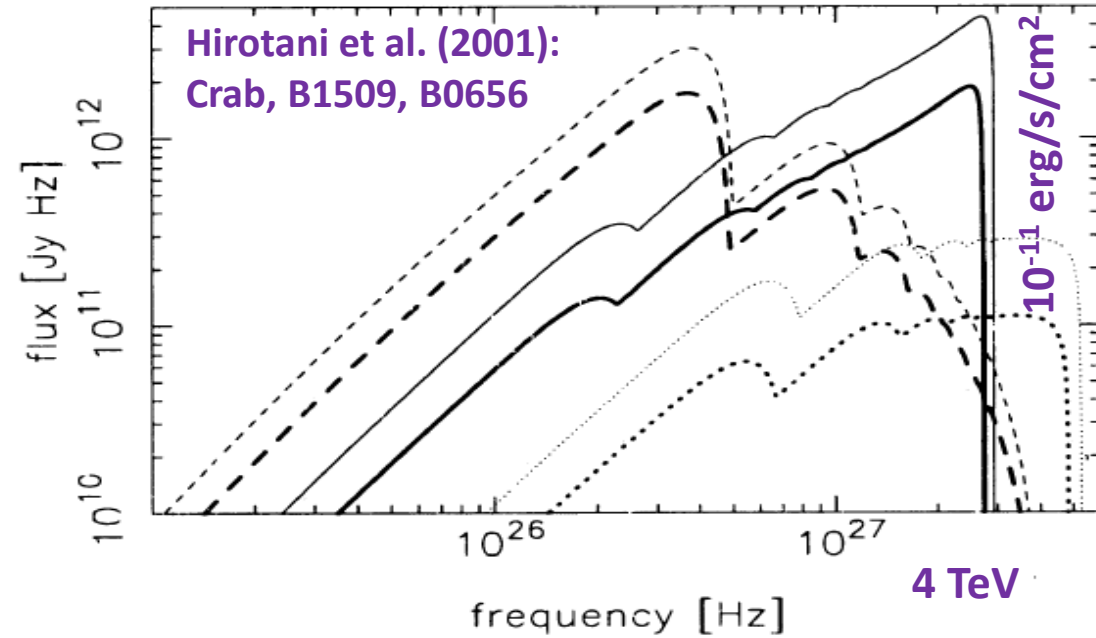
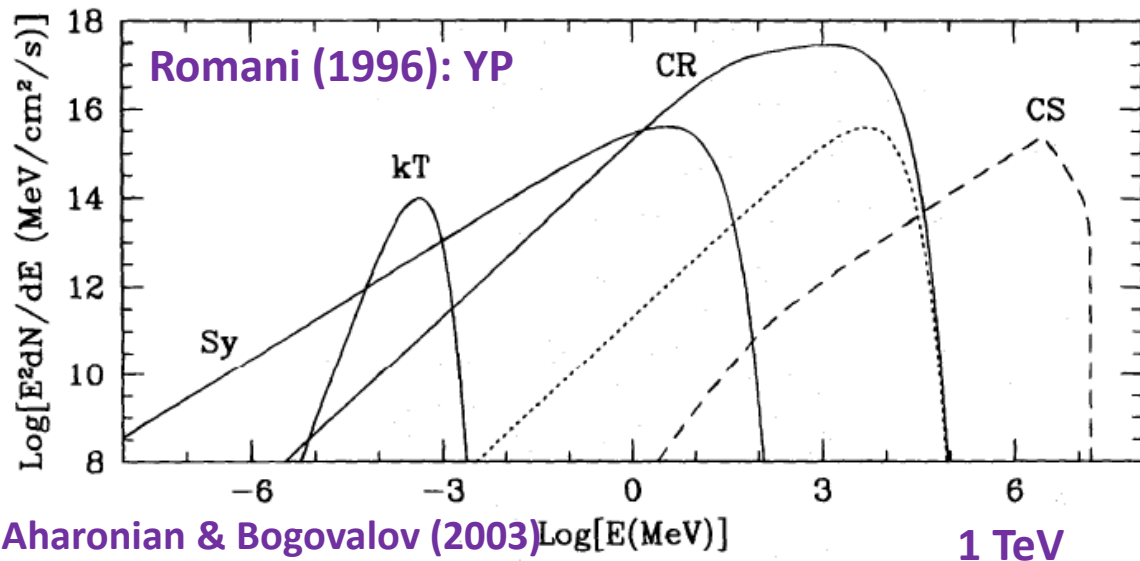
<https://www.nasa.gov/feature/goddard/2018/pulsar-in-a-box-reveals-surprising-picture-of-a-neutron-star-s-surroundings>



# Expectations: TeV Pulsed Emission?

## Early OG models

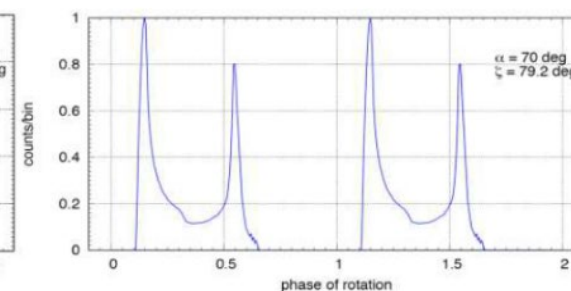
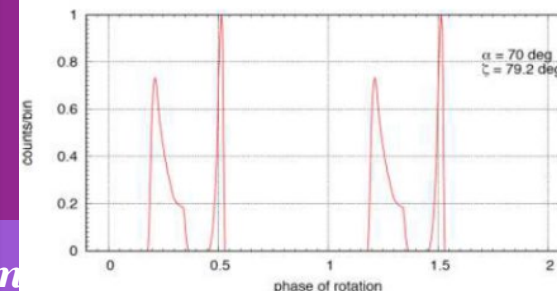
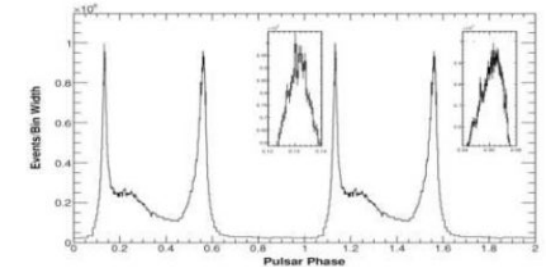
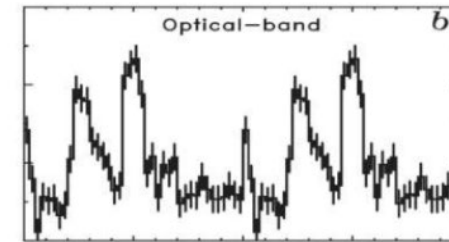
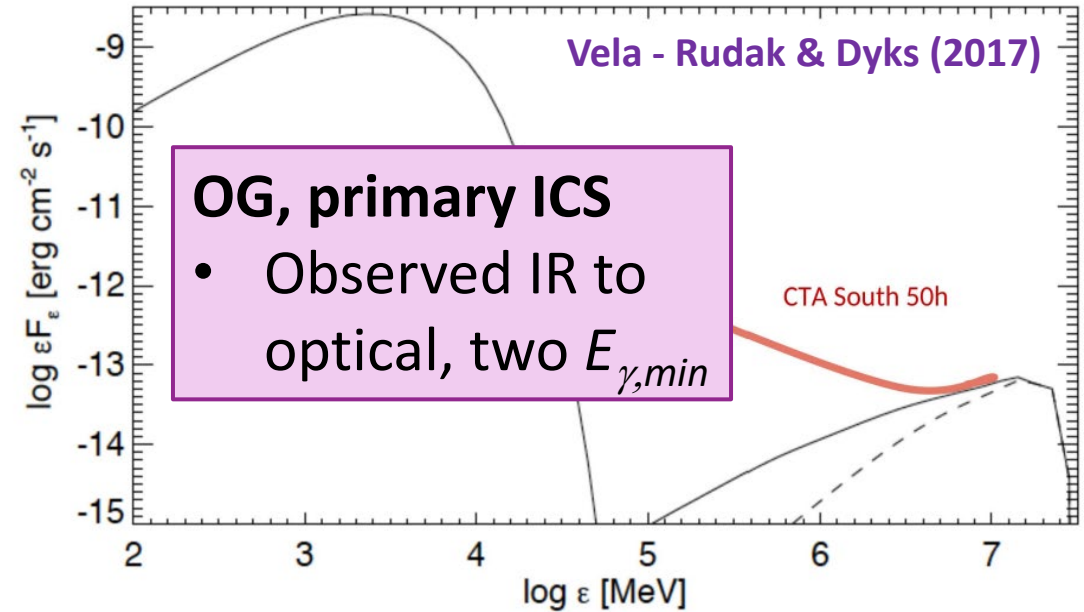
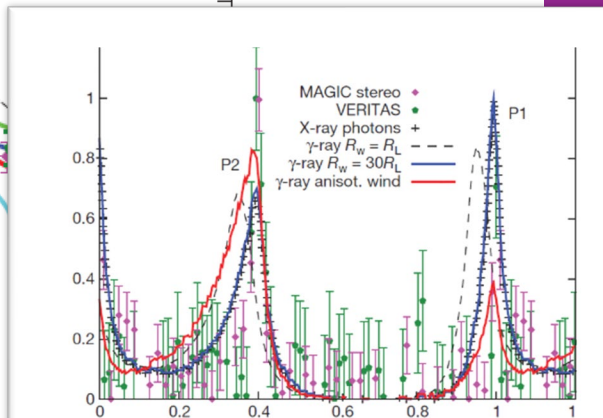
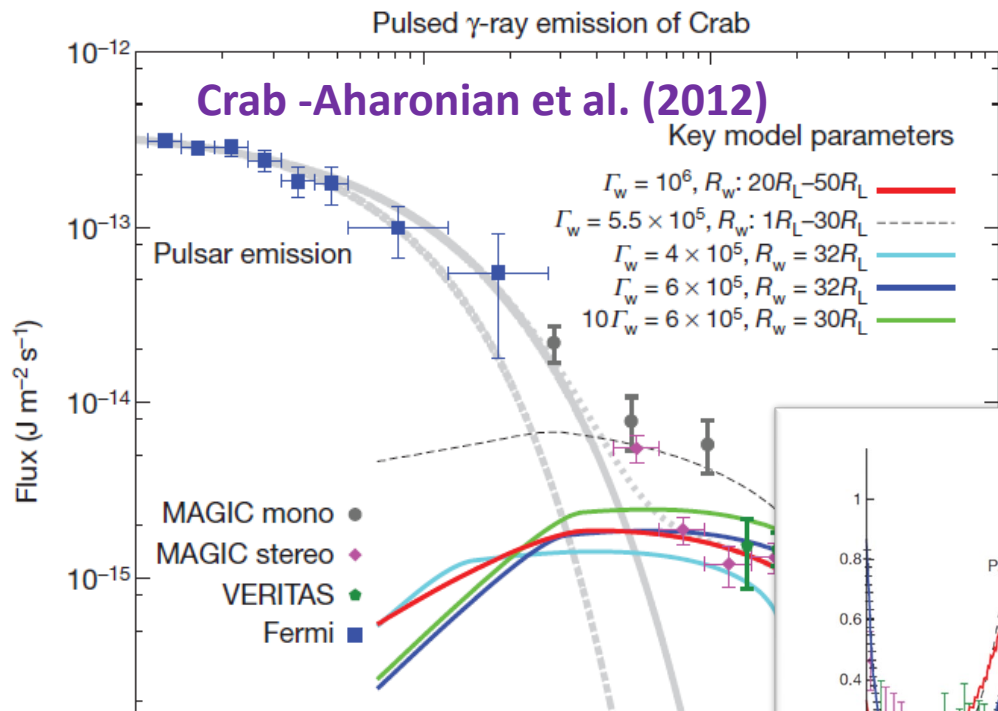
- Primaries scattering SR by pairs [or observational IR spectrum]
- Natural TeV bump at <1% - 5% of GeV flux
- Magnetic or two-photon pair production?



# Expectations: TeV Pulsed Emission?

## Cold, relativistic wind model

- Conversion of Poynting flux to kinetic energy
- $20 - 50 R_{LC}$
- Observed X-rays as soft photons



Bogovalov & Aharonian (2000)

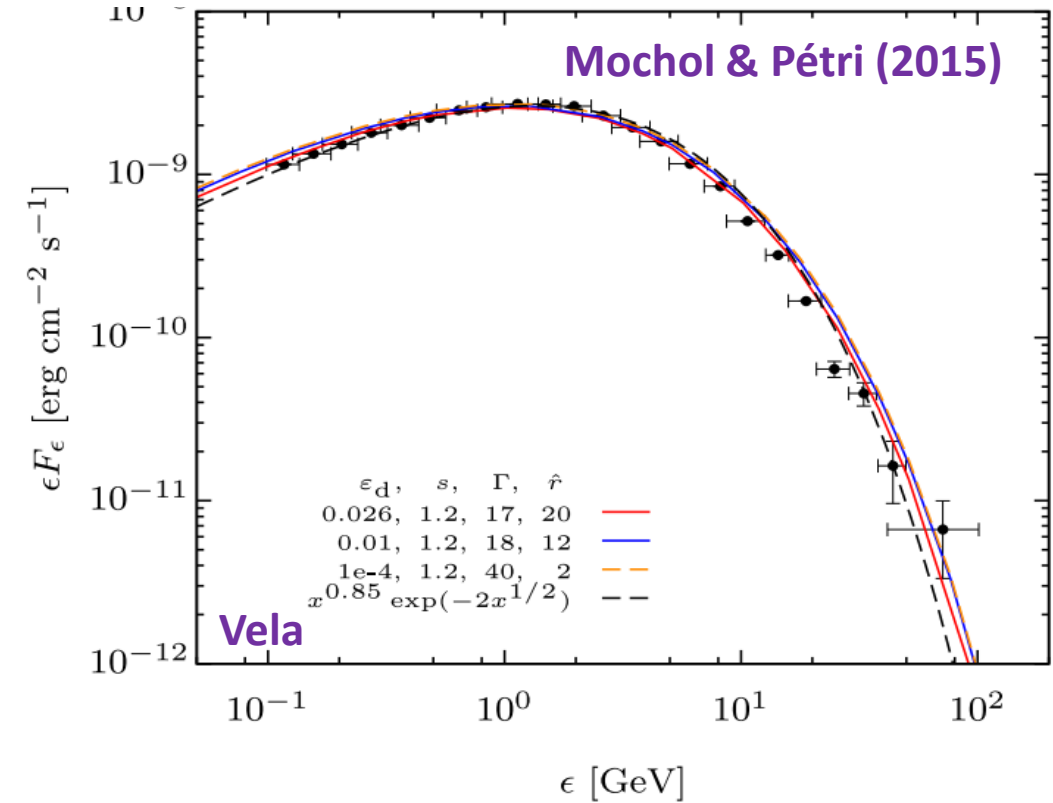
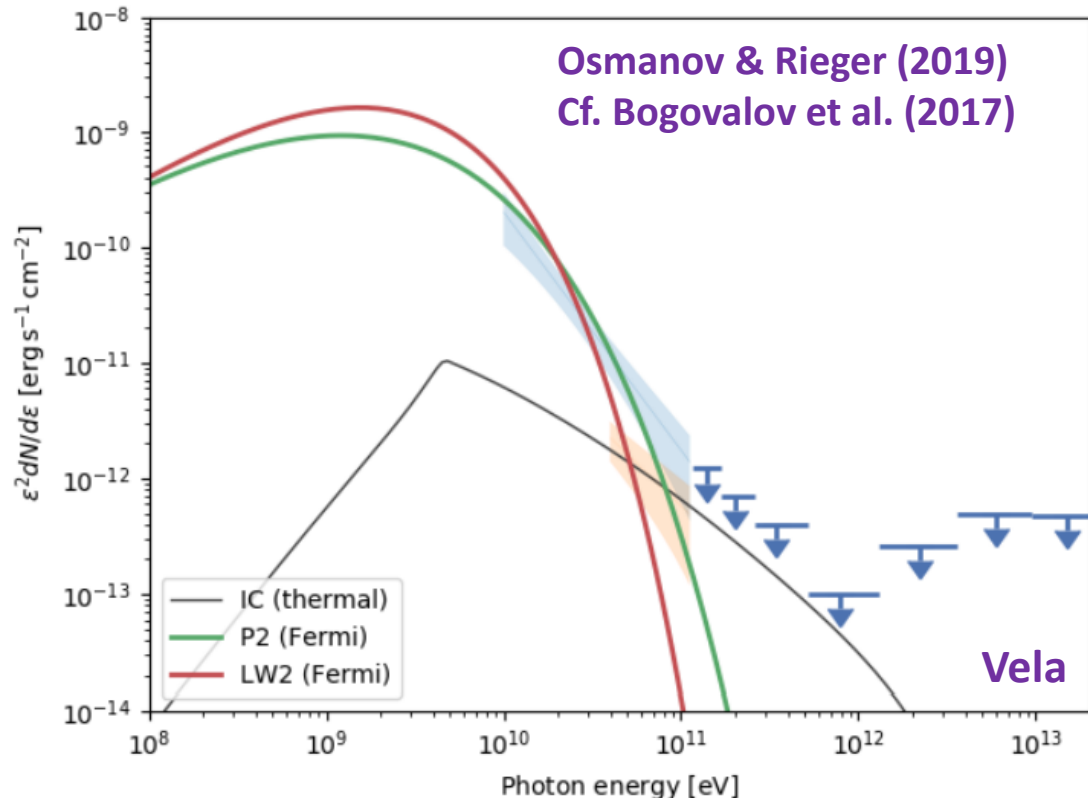
Bogovalov et al. (2017)



# Expectations: TeV Pulsed Emission?

**Magneto-centrifugal (rotationally-driven) particle acceleration**

- ICS on thermal surface photons ( $T \sim 10^6 \text{K}$ )



**CS / Striped-wind models**

- SR in CS (magnetic reconnection)
- SSC component detectable in Crab, not Vela

# Expectations: TeV Pulsed Emission?

## SSC by pairs

- Crab
- Energetics / spectra in ballpark of VERITAS results

Lyutikov (2012)

$$\epsilon_{\gamma,p} \approx \gamma_p m_e c^2 = 150 \text{ GeV } \eta_{-2}^{1/4} \sqrt{\xi} \lambda_2^{-1}$$

$$L_{\text{KN},p} = \lambda L_{\text{KN},b} = 4 \times 10^{35} \eta_{G,-1} \epsilon_{\text{UV},0}^{-2} \lambda_2$$

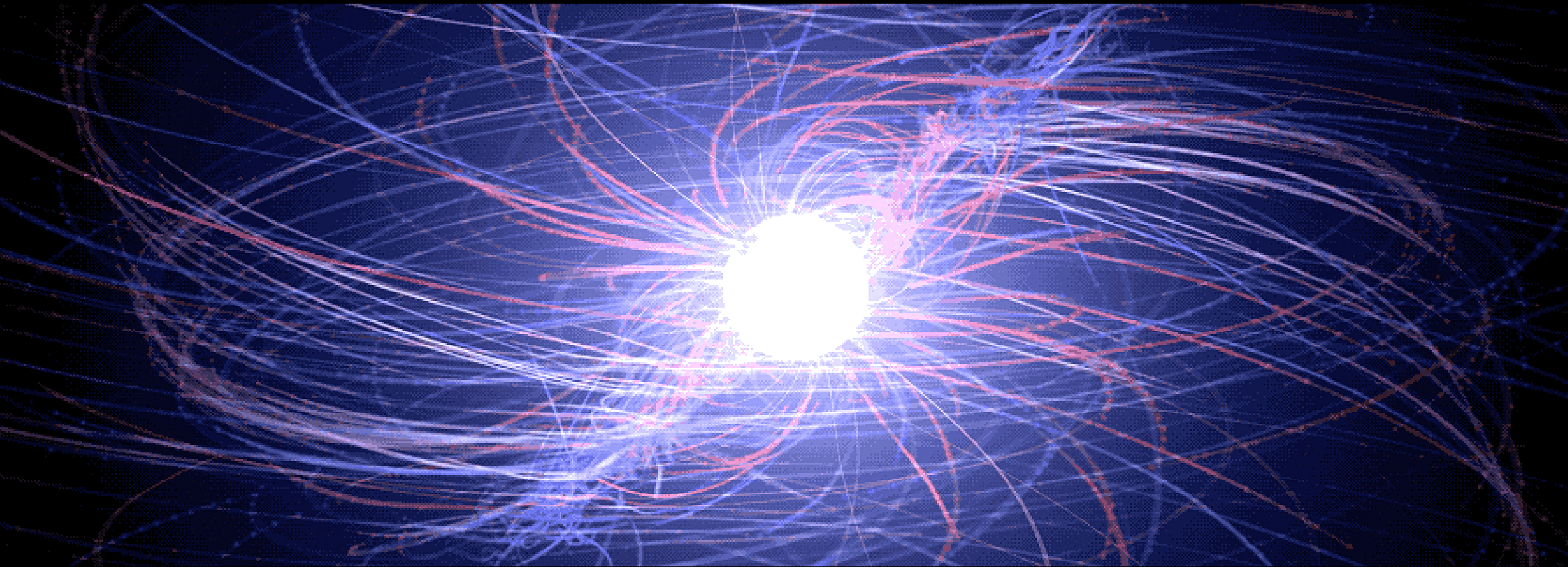


## Cyclotron-self-Compton

- Counter-streaming beams on OG
- Outward beam: Doppler-boosted cyclotron emission (high  $M_+ \sim 10^6 - 10^7$ )
- Inward beam: ICS on cyclotron photons

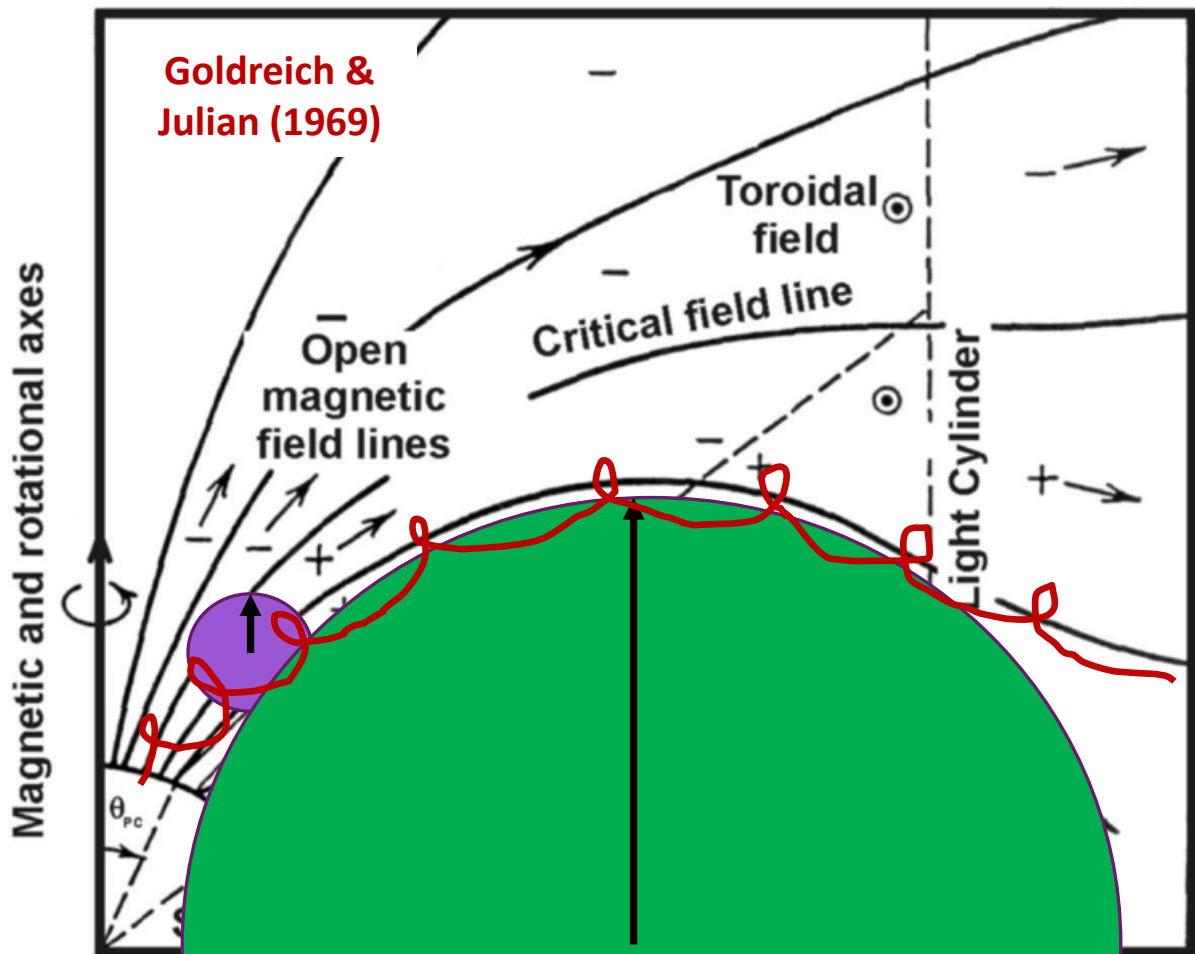
# Separatrix / CS Model

<https://www.nasa.gov/feature/goddard/2018/pulsar-in-a-box-reveals-surprising-picture-of-a-neutron-star-s-surroundings>



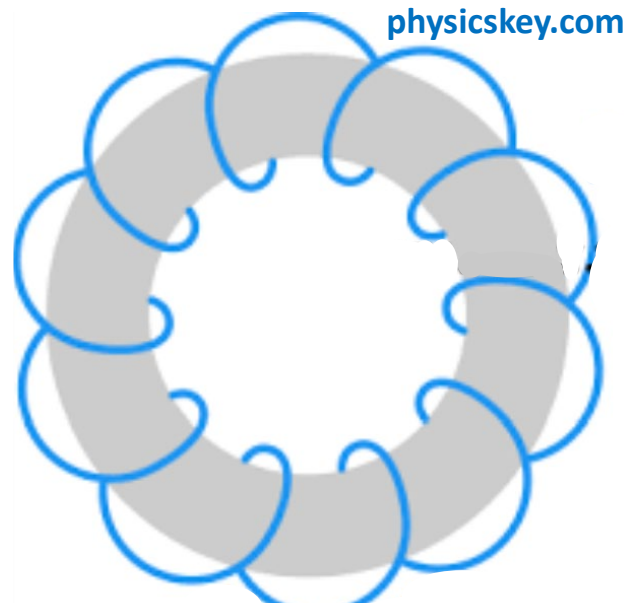
# Synchro-Curvature Radiation

Cf. talk by Viganò



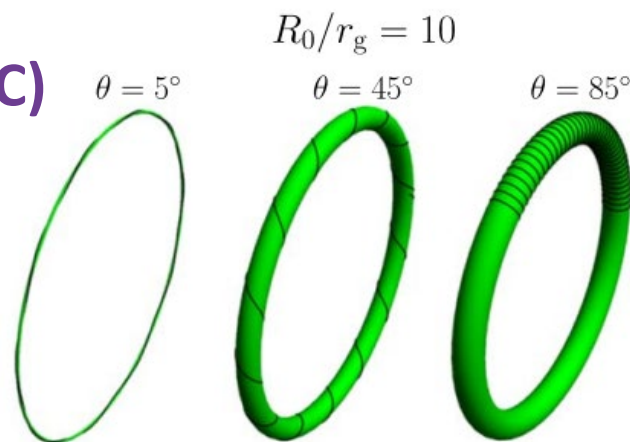
- Perpendicular: SR
- Parallel: CR

Synchro-curvature (SC)



Cheng & Zhang (1996)

Kalapocharakos et al. (2023)



Cerutti et al. (2016)

$$F_\nu(\nu) = \frac{\sqrt{3}e^3\tilde{B}_\perp}{m_e c^2} \left(\frac{\nu}{\nu_c}\right) \int_{\nu/\nu_c}^{+\infty} K_{5/3}(x) dx$$

$$\tilde{B}_\perp = \sqrt{(\mathbf{E} + \boldsymbol{\beta} \times \mathbf{B})^2 - (\boldsymbol{\beta} \cdot \mathbf{E})^2}$$

$$\nu_c = \frac{3e\tilde{B}_\perp\gamma^2}{4\pi m_e c}$$

# Synchro-Curvatures Radiation

- Encapsulates 2 limits: CR, SR
- “Magnetic brehmsstrahlung”



Cheng & Zhang (1996)  
 Zhang, Xia & Yang (2000)  
 Kelner & Aharonian (2012)  
 Prosekin, Kelner & Aharonian (2013)  
 Kelner et al. (2015)  
 Viganò et al. (2015)  
 Cerutti et al. (2016)  
 Torres (2018)  
 Íñiguez-Pascual et al. (2022a,b)

## Cutoff energy:

$$E_{\text{CR}} = \frac{3\hbar c \gamma^3}{2\rho_c} \quad \longrightarrow \quad E_c(\Gamma, r_c, r_{\text{gyr}}, \alpha) = \frac{3}{2} \hbar c Q_2 \Gamma^3$$

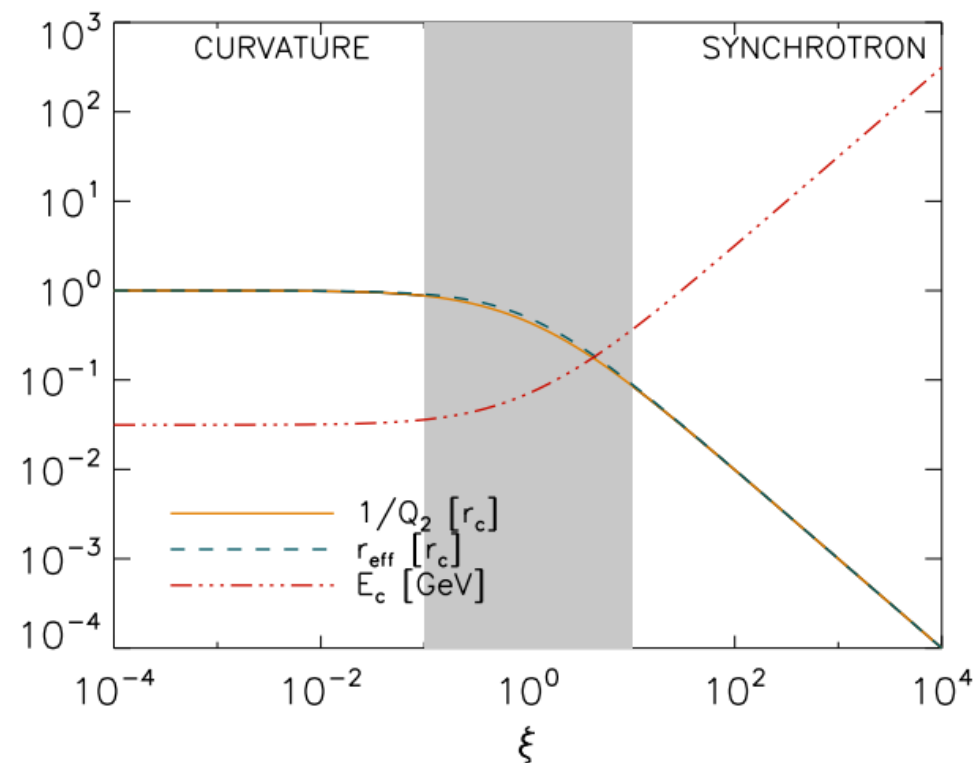
$$\xi = \frac{r_c \sin^2 \alpha}{r_{\text{gyr}} \cos^2 \alpha} \quad Q_2^2 = \frac{\cos^4 \alpha}{r_c^2} \left[ 1 + 3\xi + \xi^2 + \frac{r_{\text{gyr}}}{r_c} \right]$$

## Total power:

$$\int \left( \frac{dP}{dE} \right)_{\text{CR}} dE = -\frac{2e^2 c \gamma^4}{3\rho_c^2} \quad \longrightarrow \quad P_{\text{sc}} = \frac{2(Ze)^2 \Gamma^4 c}{3r_c^2} g_r$$

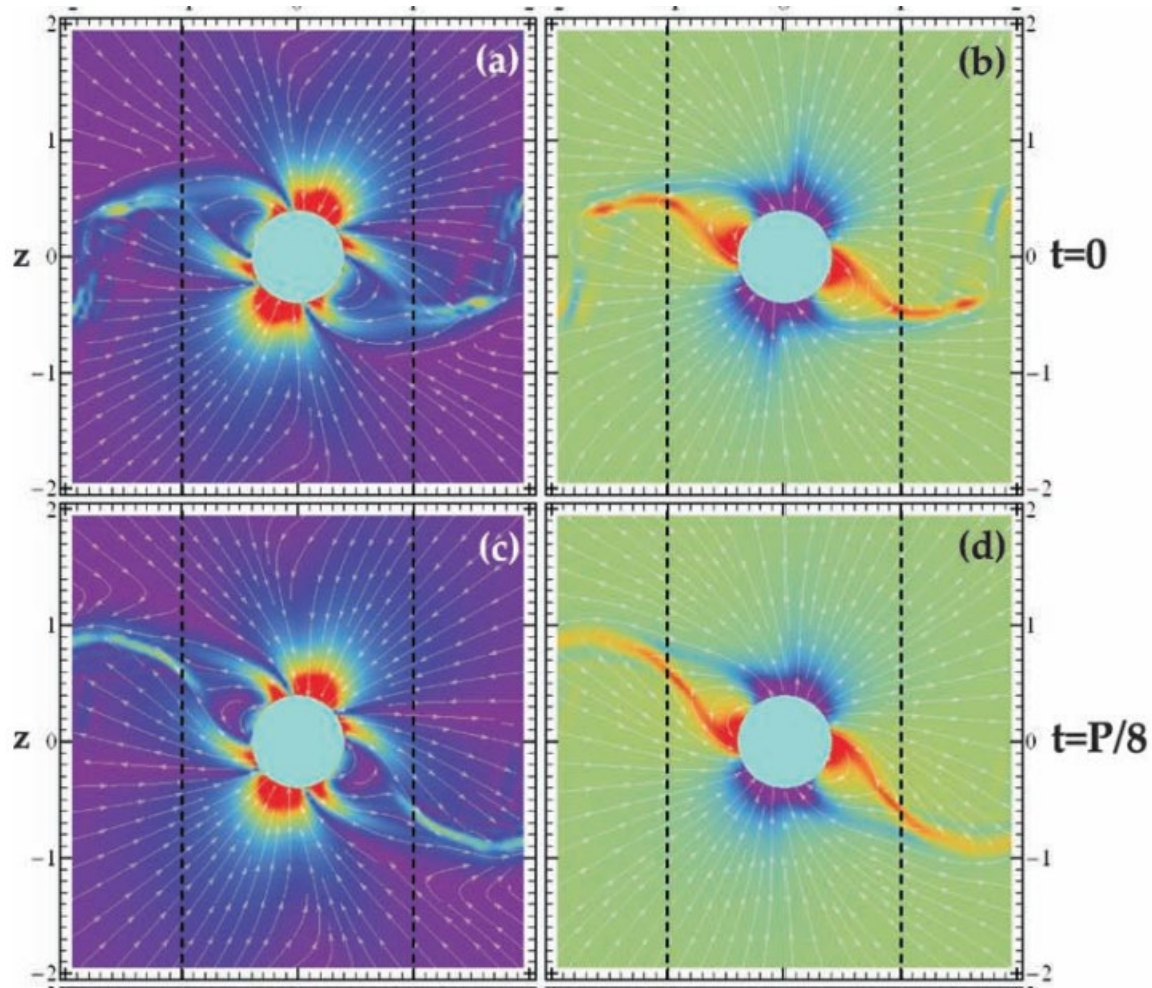
$$g_r = \frac{r_c^2 [1 + 7(r_{\text{eff}} Q_2)^{-2}]}{r_{\text{eff}}^2 8(Q_2 r_{\text{eff}})^{-1}}$$

$$\frac{dP_{\text{sc}}}{dE} = \frac{\sqrt{3}e^2 \Gamma E}{4\pi \hbar r_{\text{eff}} E_c} [(1+z)F(y) - (1-z)K_{2/3}(y)]$$

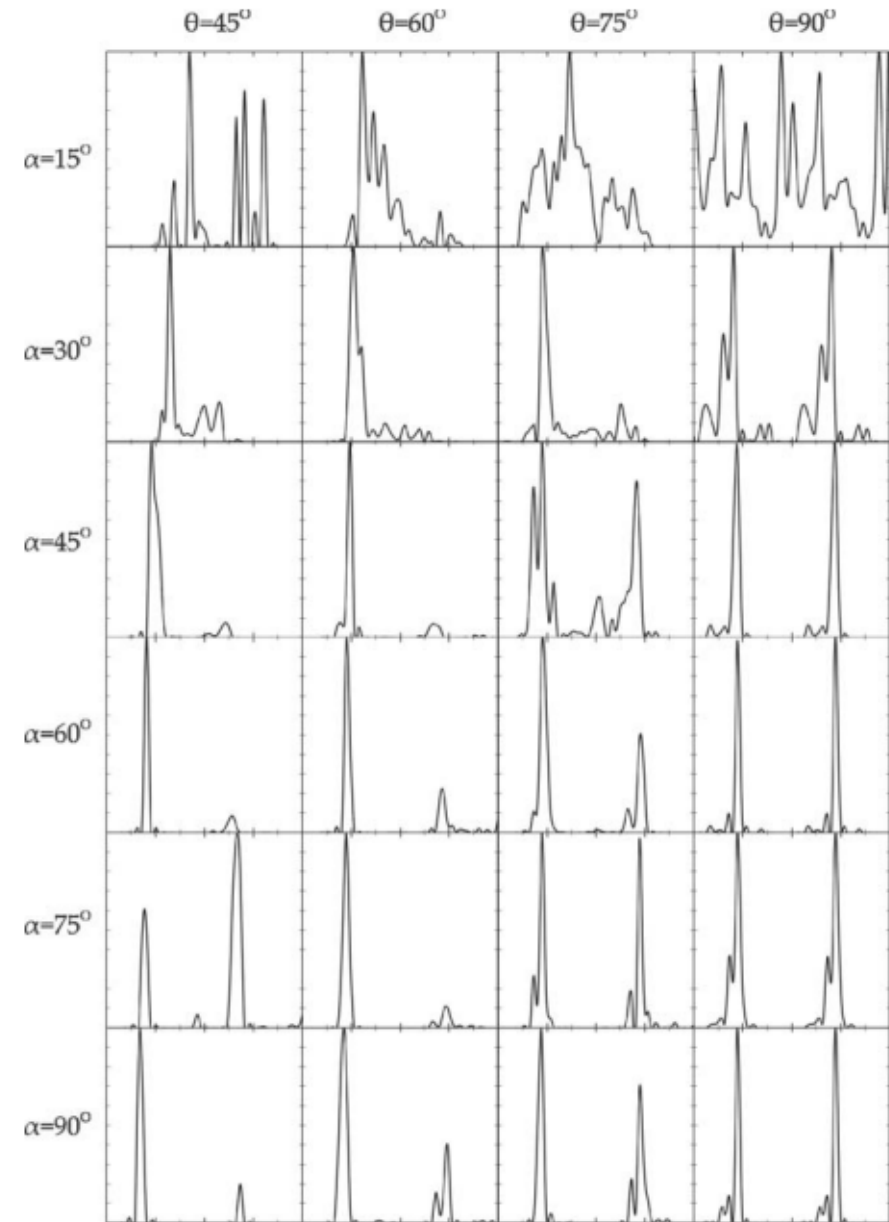


# Curvature Radiation from the CS

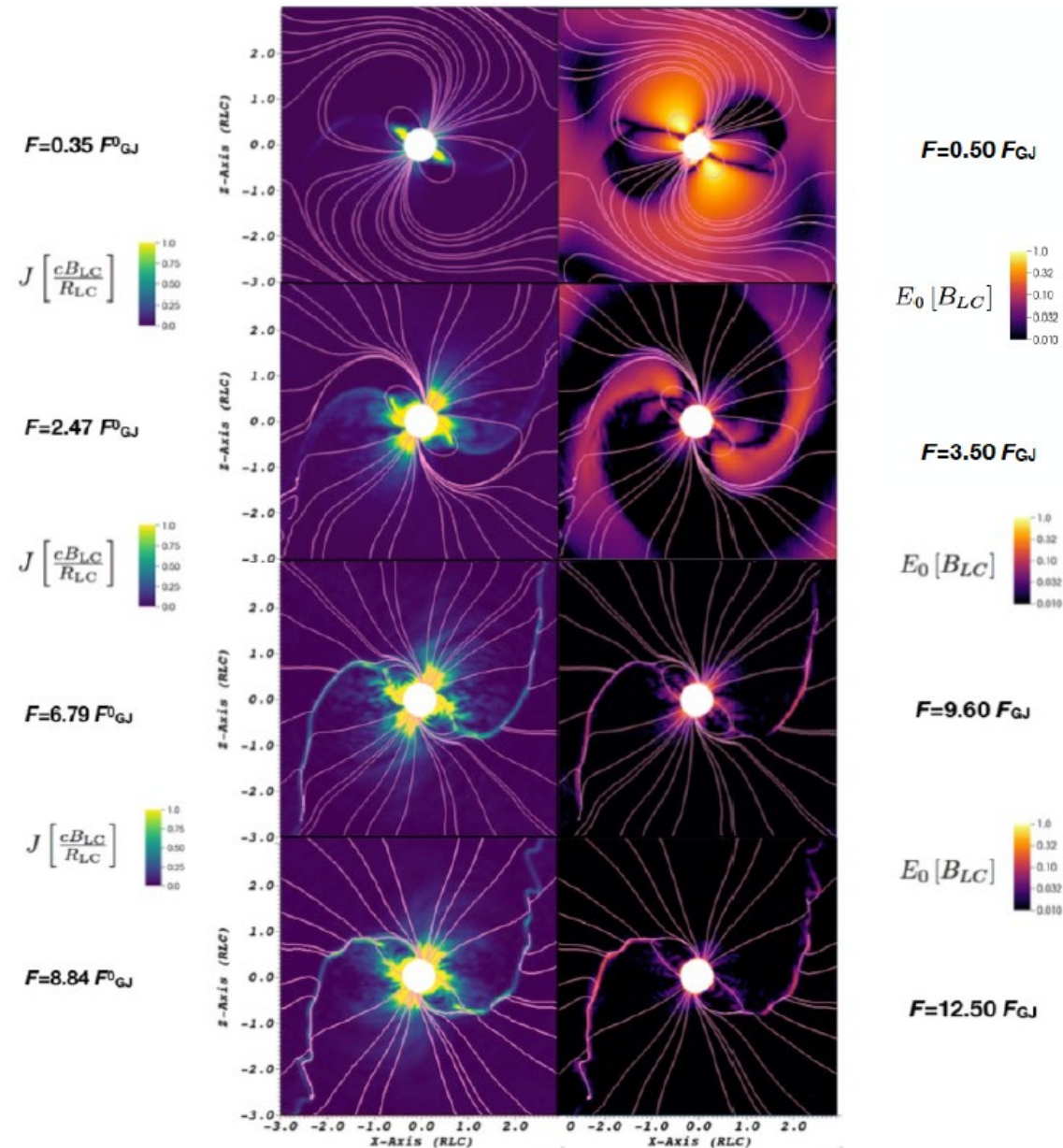
- Force-free MHD simulations indicated strong currents at tip of closed field line region and into CS
- CR from relativistic electrons / positrons in CS



Contopoulos &  
Kalapotharakos  
(2010)



# Global PIC Models



Chen & Belodorodov (2014)  
 Philippov & Spitkovsky (2014, 2018)  
 Cerutti et al. (2016)  
 Kalapotharakos et al. (2018, 2023)  
 Brambilla et al. (2018)

- Most dissipation takes place near separatrix and CS
- $E$ -field shrinks to CS as injection rate increases
- Scaling up of  $B < 10^6$  G and  $\gamma < 10^3$  [or hybrid models]

Cf. talks by Philippov, Cerutti, etc.

# Fundamental Plane

1) Radiation-Reaction Limit Regime

2) At the ECS near the LC

CR

Kalapothisarakos et al.

$$R_C \propto R_{LC} \propto P$$

$$B_{LC} \propto B_* R_{LC}^{-3} \propto B_* P^{-3}$$

$$\gamma_L \propto \epsilon_{cut}^{1/3} P^{1/3}$$

$$E_{BLC} B_{LC} \propto \gamma_L^4 R_C^{-2}$$

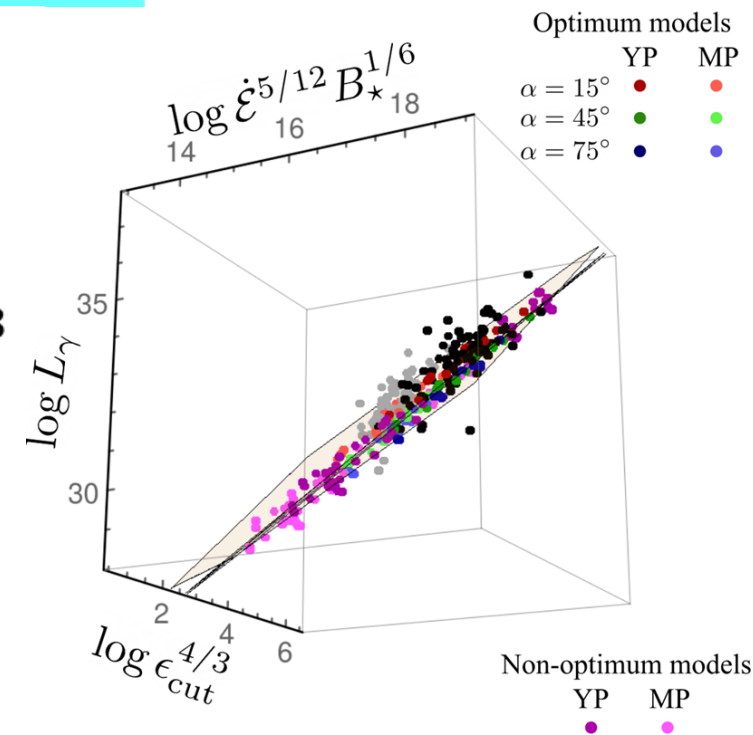
$$E_{BLC} \propto \epsilon_{cut}^{4/3} P^{7/3} B_*^{-1}$$

$$L_{\gamma 1} \propto \epsilon_{cut}^{4/3} P^{-2/3}$$

$$\rho_{GJ} \propto B_* P^{-1}$$

$$\dot{\mathcal{E}} \propto B_*^2 P^{-4}$$

$$L_{\gamma} \propto \epsilon_{cut}^{4/3} B_*^{1/6} \dot{\mathcal{E}}^{5/12}$$

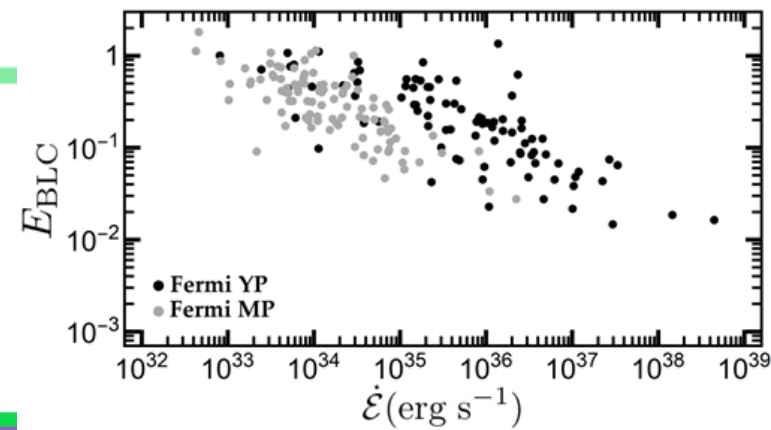


$$R_C \propto r_g \propto \gamma_L B_*^{-1} P^3$$

Kalapothisarakos et al.  
(2019, 2022, 2023)

$$L_{\gamma} \propto \epsilon_{cut} \dot{\mathcal{E}}$$

SR

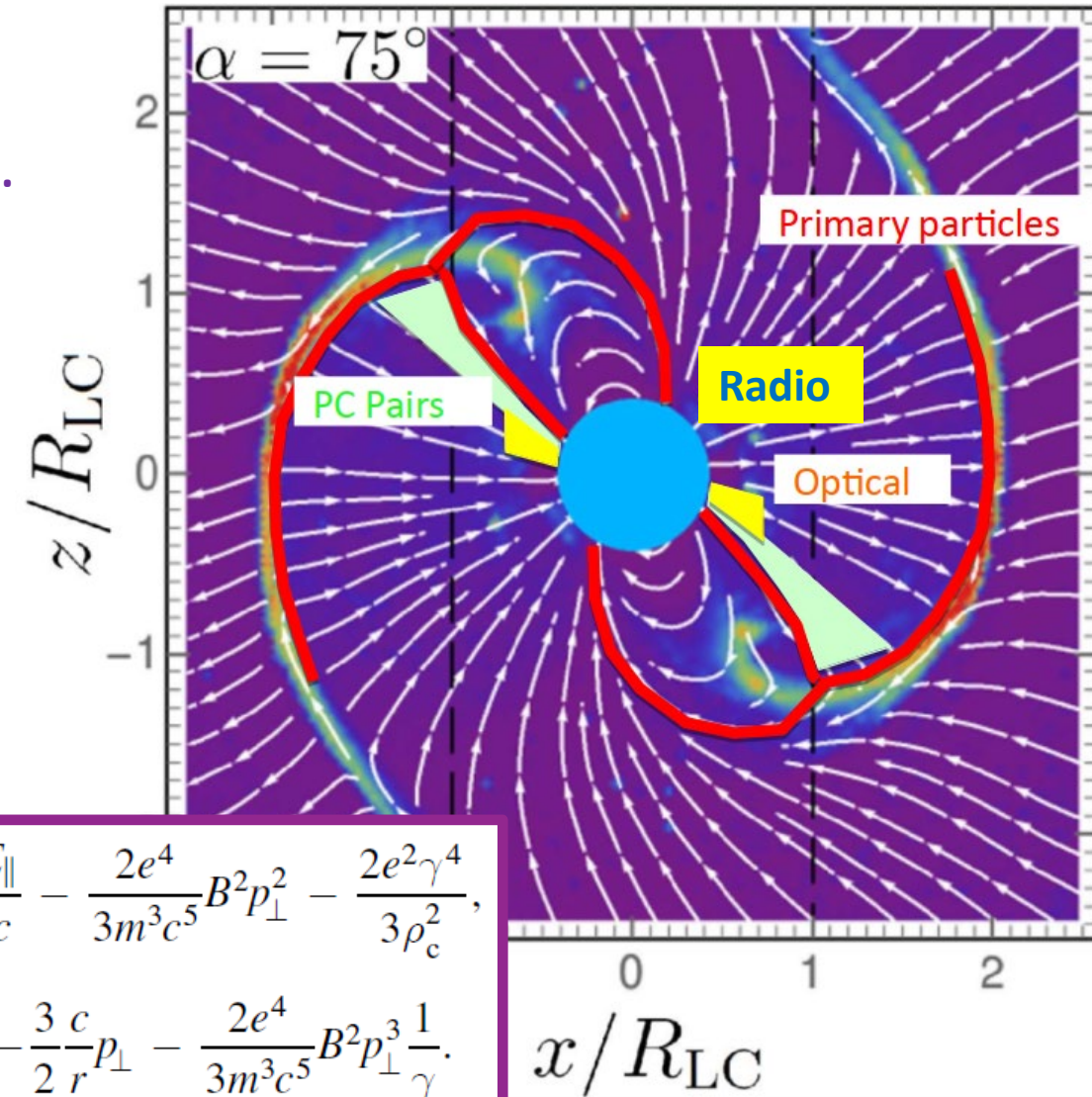




# Separatrix / CS Emission Model

Harding & Kalapotharakos (2015), Harding et al. (2018, 2021)

- Force-free magnetosphere.
- Primaries ( $\gamma_{inj} \sim 10^2$ ) from PC; pairs ( $\gamma_e \sim 10^5$ ) from cascade in offset-PC  $B$ -field (Harding & Muslimov 2011a,b).
- Primaries accelerated only near separatrix and predominantly in CS (out to  $r = 2R_{LC}$ ) assuming a constant or two-step  $E$ -field (reaching  $\gamma_e \sim 10^7$ ).
- No pair acceleration. Free primary / pair multiplicities  $M_+$ . Injection at  $\phi_{PC}$  where  $J/J_{GI} < 0$ .
- Empirical radio core / cone model. Resonant cyclotron absorption of radio photons by pairs (cf. Lyubarski & Petrova 1998).
- Solve particle dynamics in observer frame.
- SC (CR+SR), ICS, SSC radiation mechanisms.



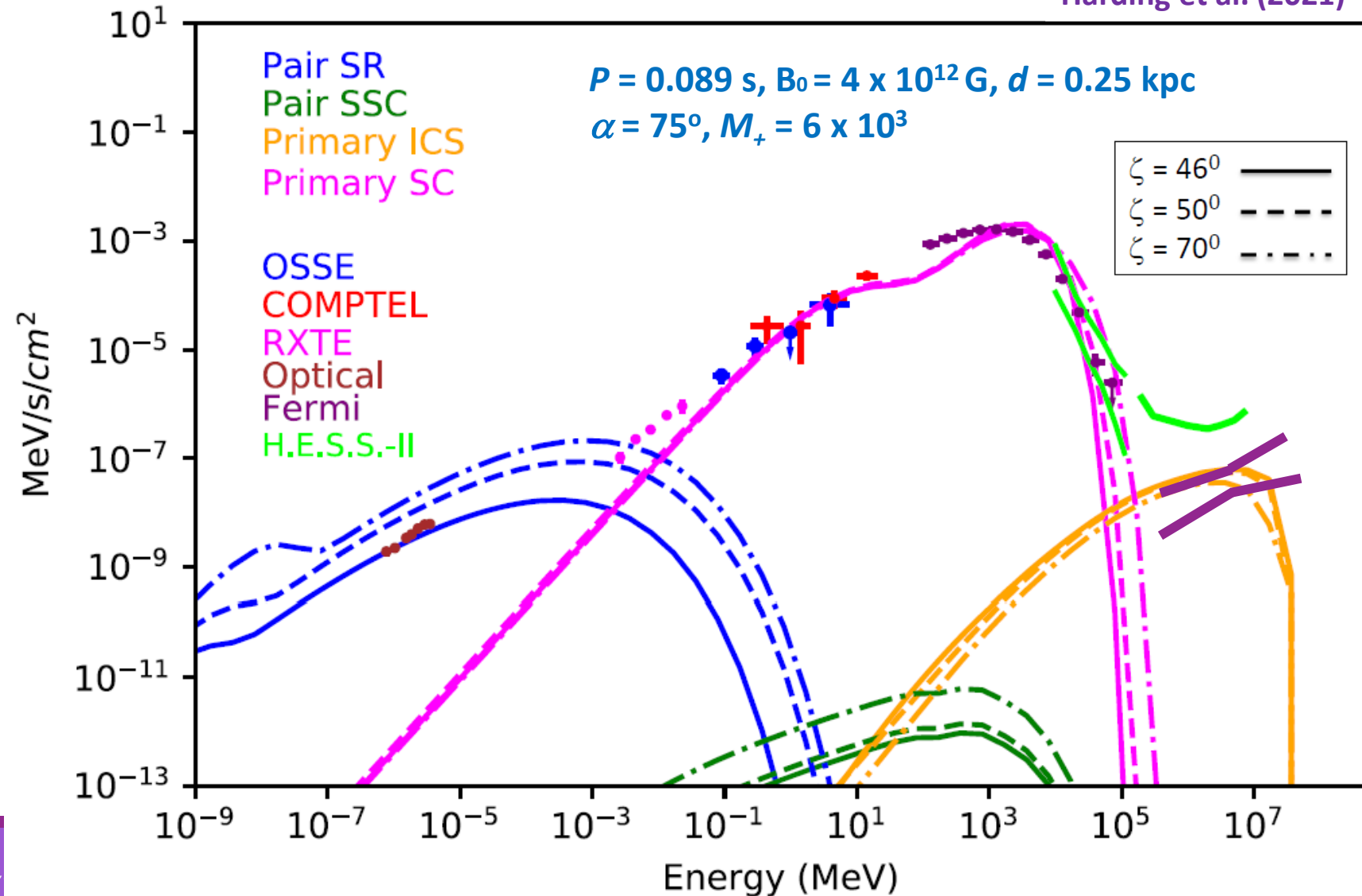
$$\frac{d\gamma}{dt} = \frac{eE_{\parallel}}{mc} - \frac{2e^4}{3m^3c^5} B^2 p_{\perp}^2 - \frac{2e^2\gamma^4}{3\rho_c^2},$$

$$\frac{dp_{\perp}}{dt} = -\frac{3c}{2r} p_{\perp} - \frac{2e^4}{3m^3c^5} B^2 p_{\perp}^3 \frac{1}{\gamma}.$$

# Results: Vela Spectrum

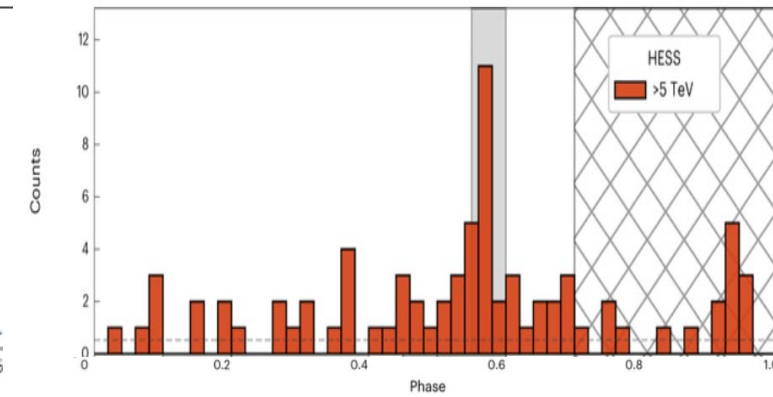
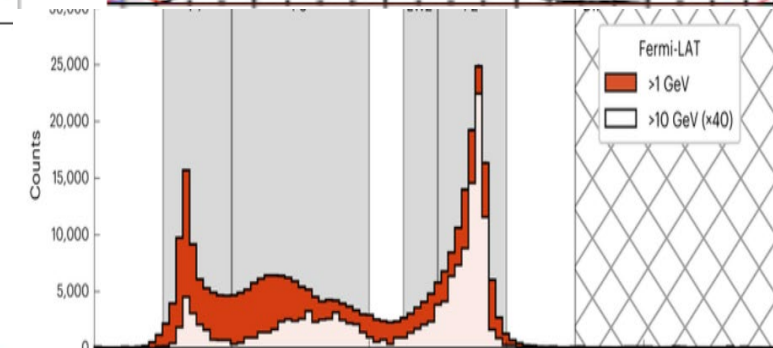
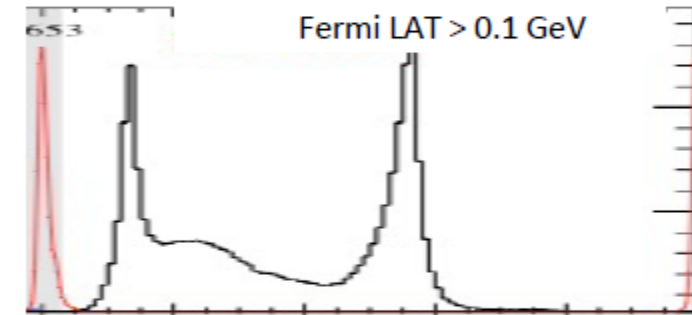
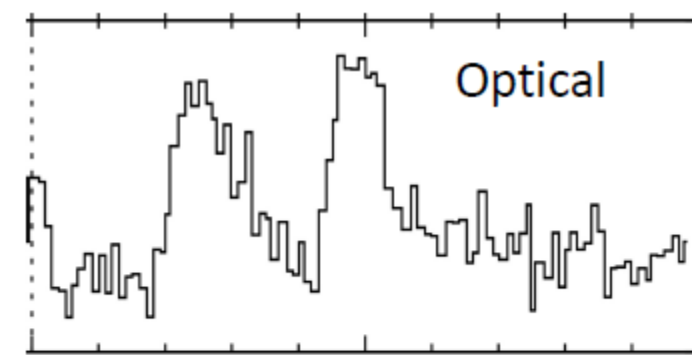
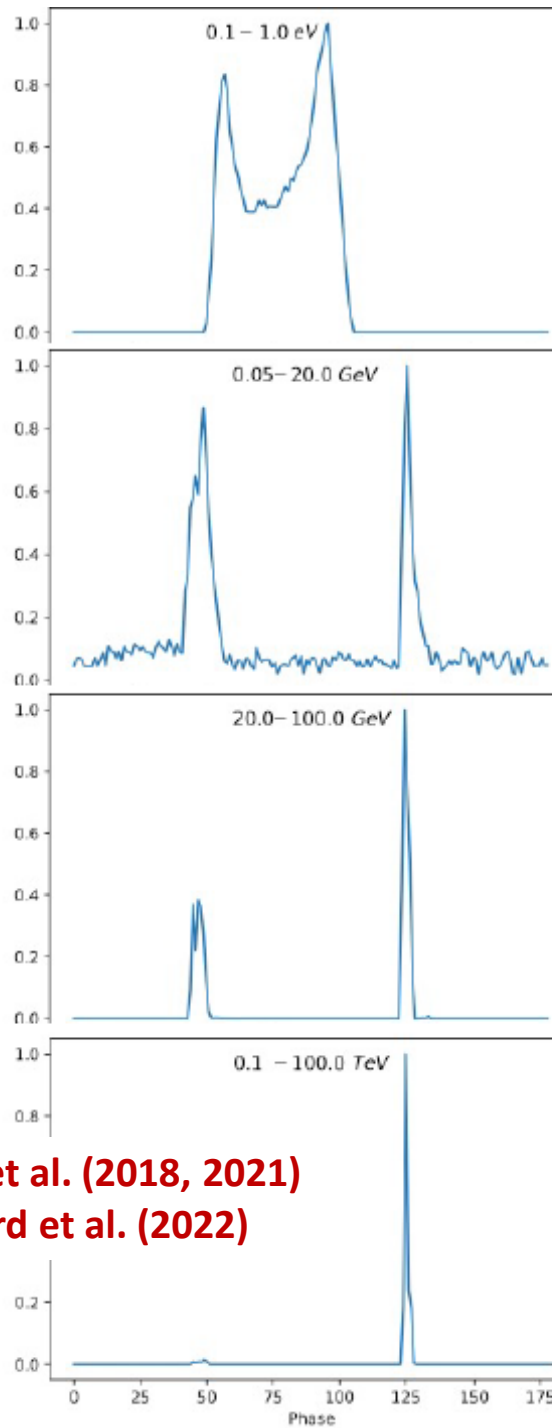
Harding et al. (2021)

- Detectable primary ICS component around 10 TeV
- Low-energy SR can boost primary ICS (T limit)
- Difference in offset-dipolar field influences primary ICS
- Pair SR matches optical data
- 10 – 100 MeV dip: More  $E$ -field variation needed
- TeV emission requires high  $\gamma_{\max}$ , pointing to CR in GeV band



# Results: Vela LCs

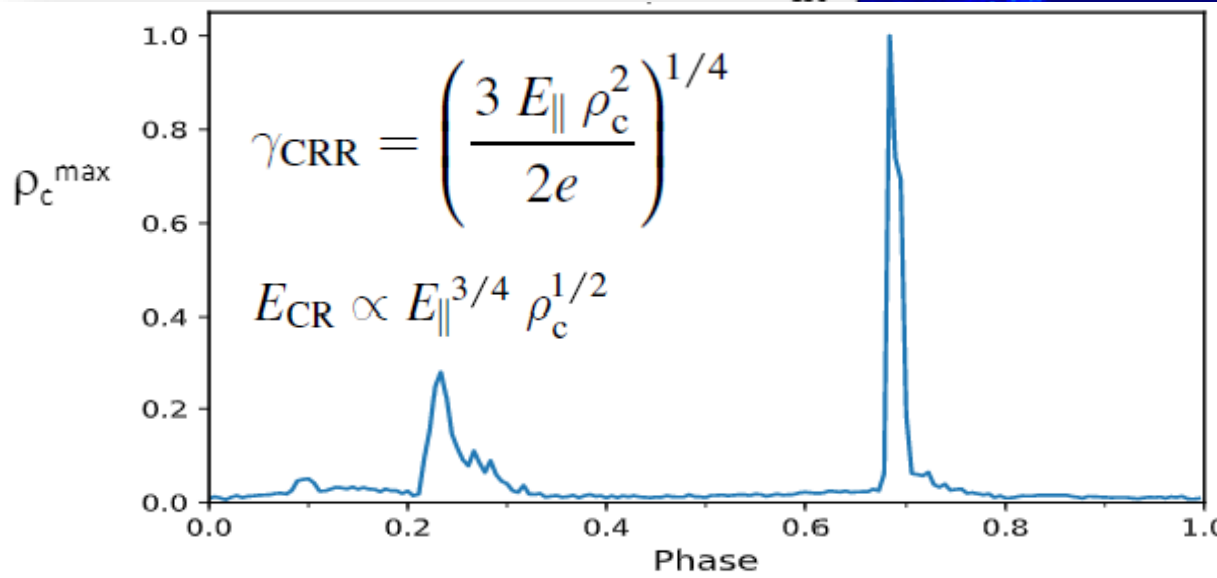
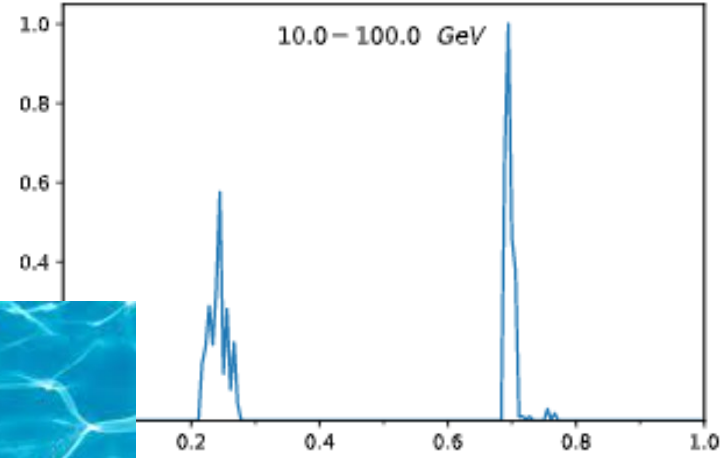
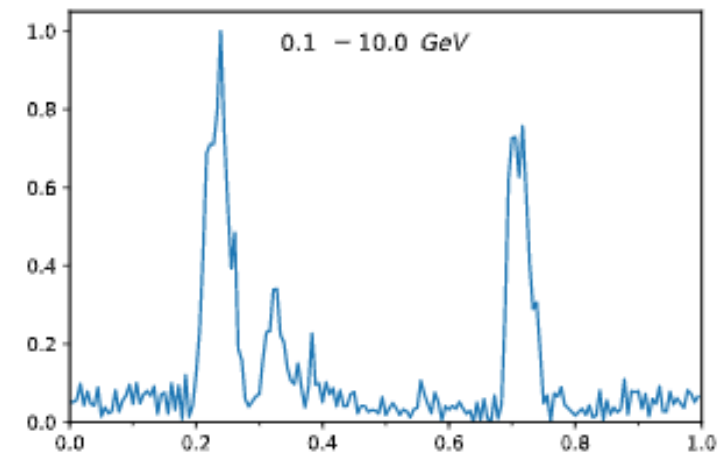
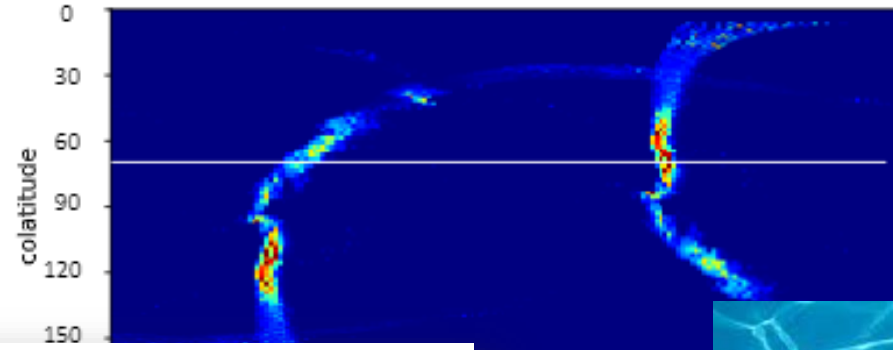
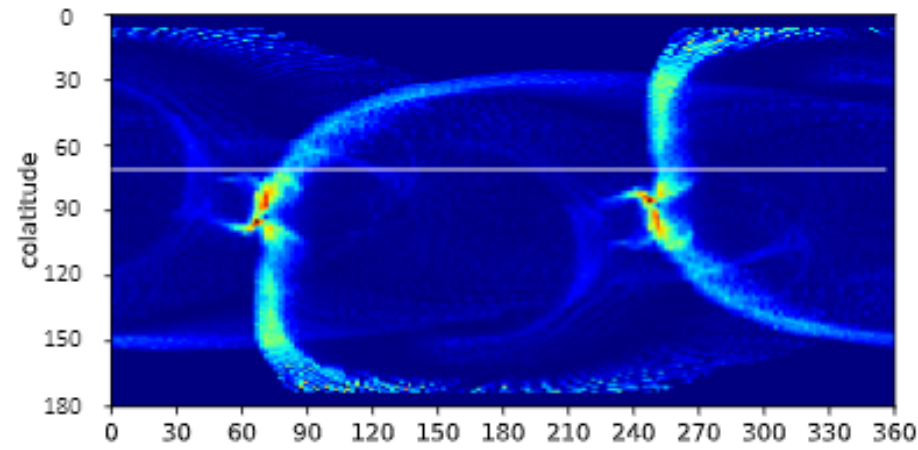
- Reasonable multi-wavelength LC predictions
- P1/P2 vs  $E_\gamma$  effect: higher-energy photons in P2 – larger  $\rho_c$
- Only P2 in TeV: highest-energy particles responsible
- Narrowing of peaks with energy
- $E_{||}(\phi)$  leading to azimuthally-dependent emissivity improves radio-to- $\gamma$  lags



Harding et al. (2018, 2021)  
Barnard et al. (2022)

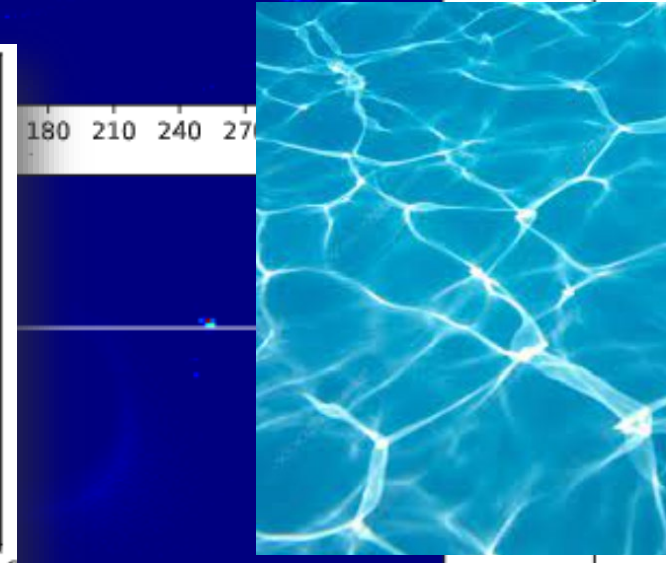
# Results: Vela LCs

- P1/P2 vs  $E_\gamma$  effect:  
higher-energy photons in P2 – larger  $\rho_c$  (near CS)
- Narrowing of peaks vs  $E_\gamma$



$$\gamma_{\text{CRR}} = \left( \frac{3 E_{\parallel} \rho_c^2}{2e} \right)^{1/4}$$

$$E_{\text{CR}} \propto E_{\parallel}^{3/4} \rho_c^{1/2}$$

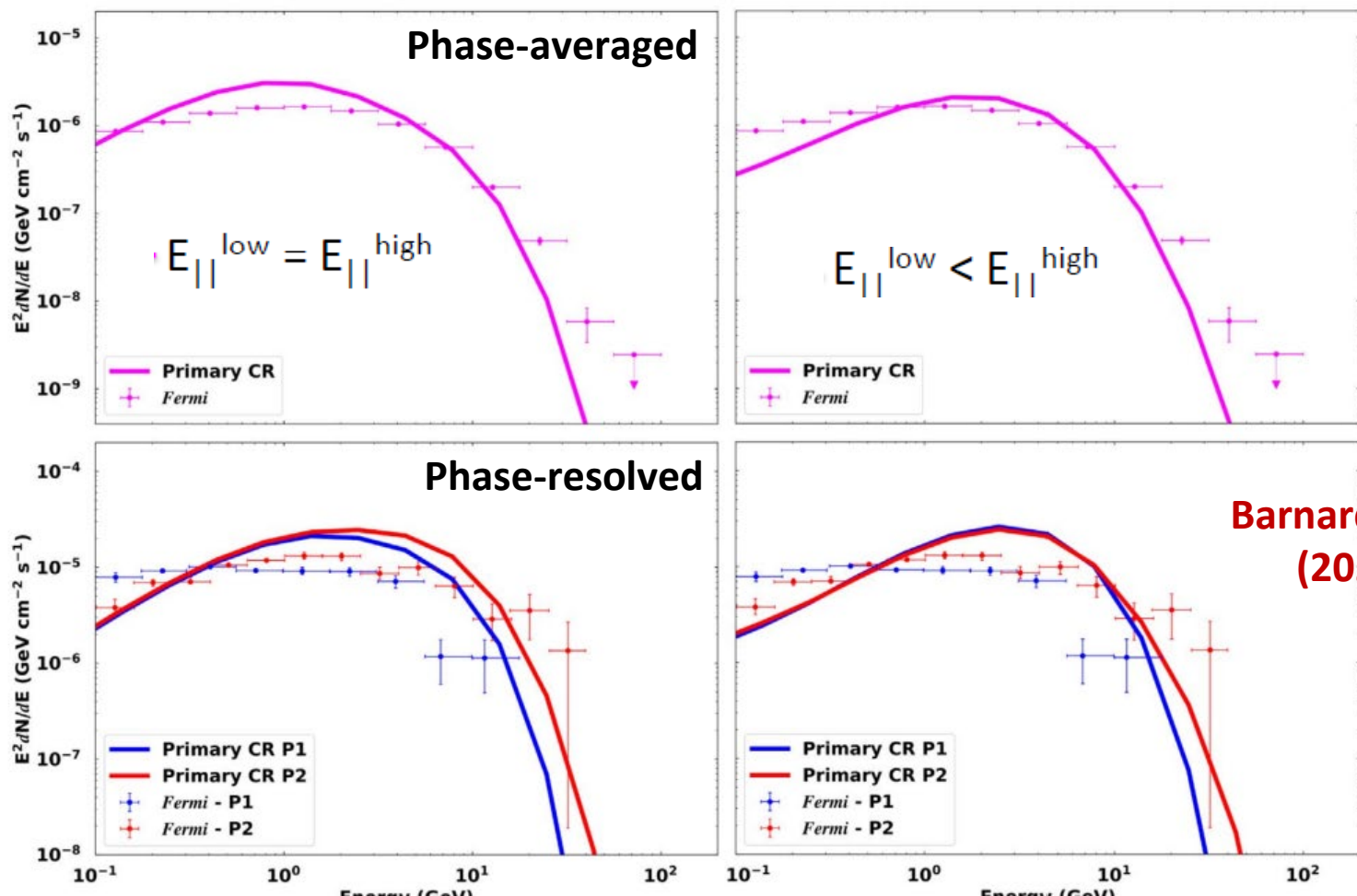


Harding et al. (2021)  
Barnard et al. (2022)

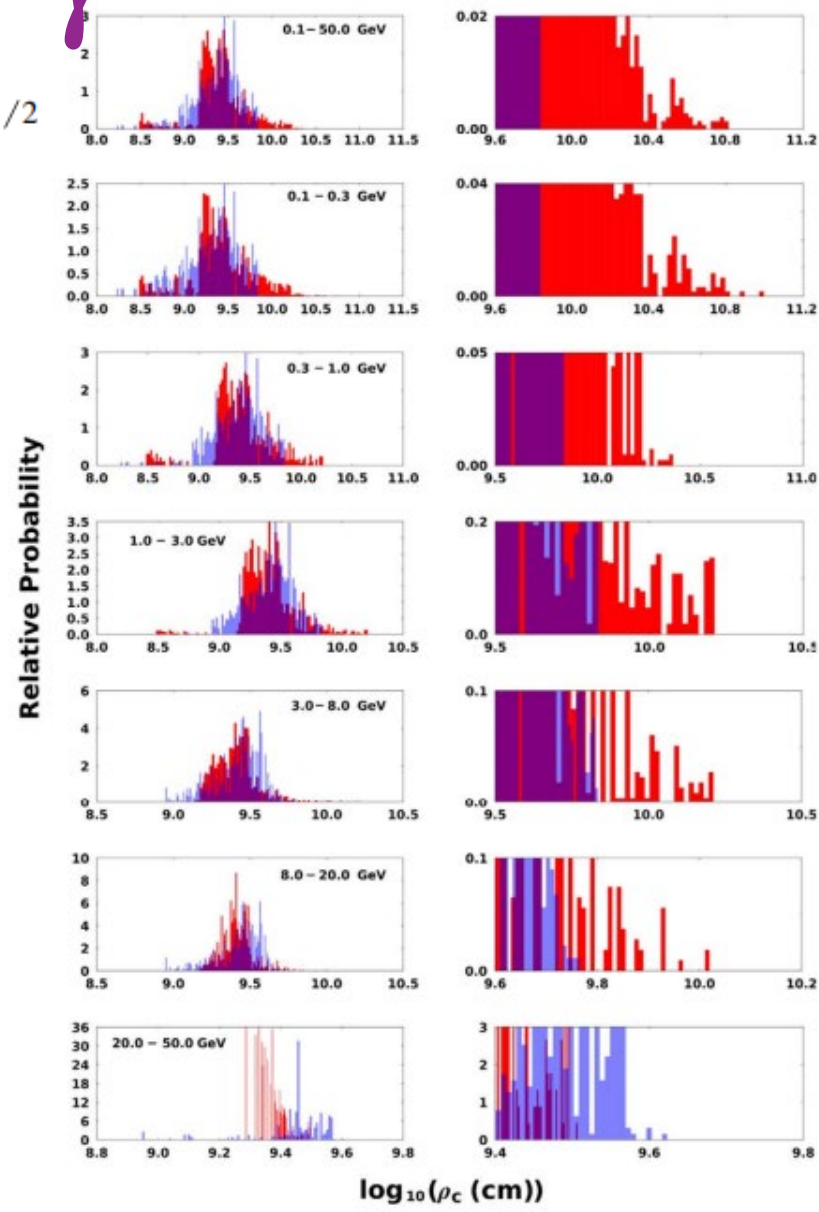
# P1/P2 vs $E_\gamma$

- Curvature radiation-reaction limit
- P2 systematically larger  $\rho_c$

$$E_{\gamma,CR} \sim 4 \left( \frac{E_{||}}{10^4 \text{ statvolt cm}^{-1}} \right)^{3/4} \left( \frac{\rho_c}{10^8 \text{ cm}} \right)^{1/2}$$



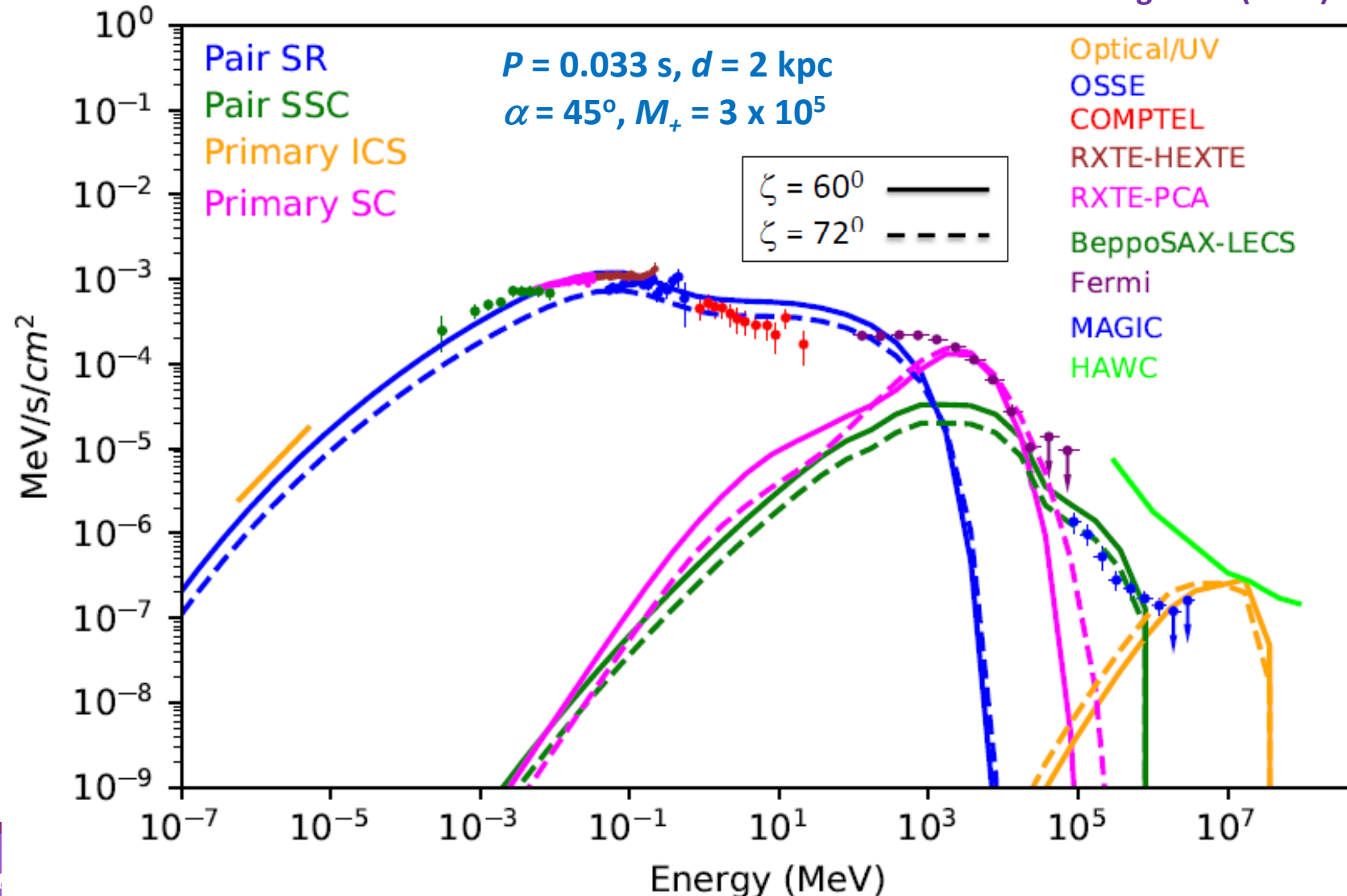
Barnard et al.  
(2022)



# Results: Crab Spectrum

Harding et al. (2021)

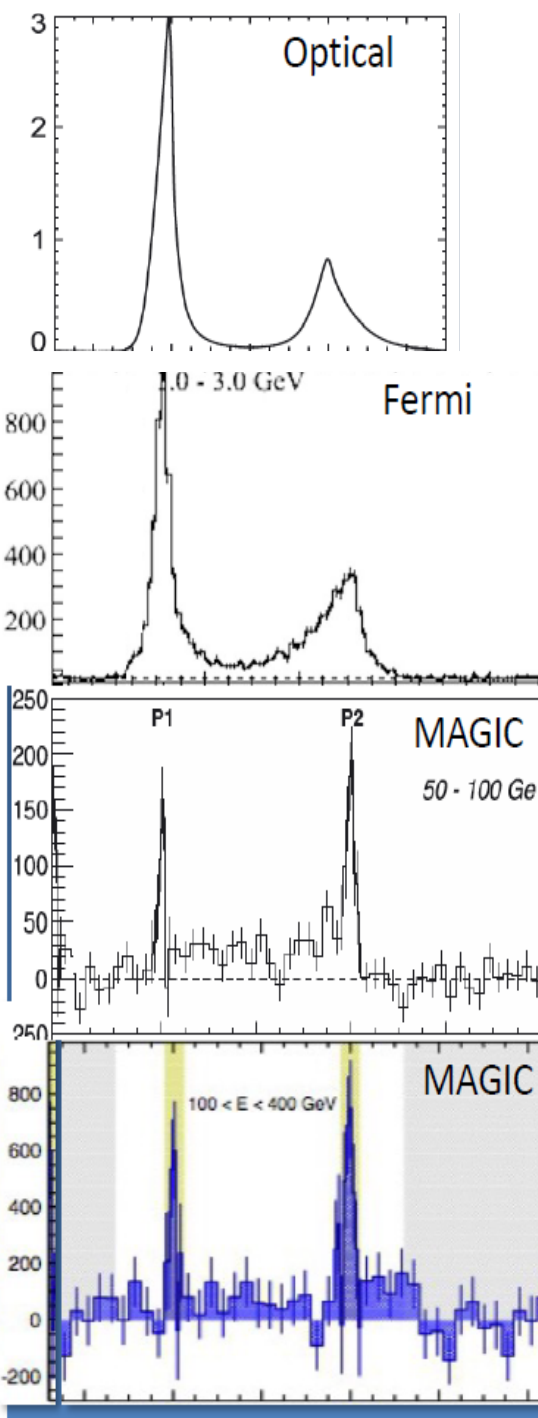
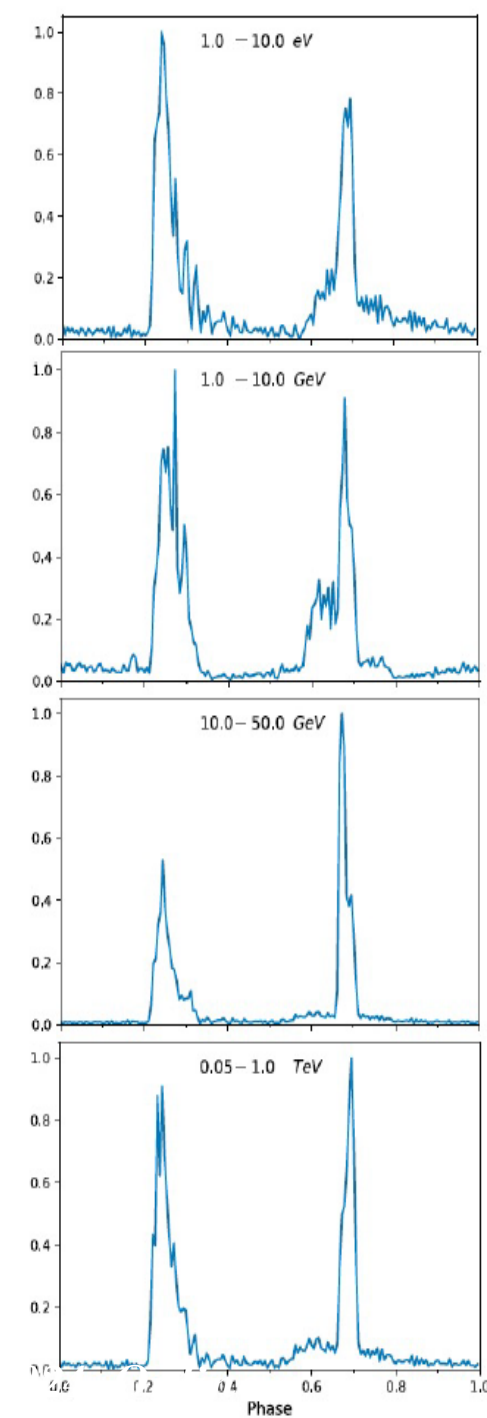
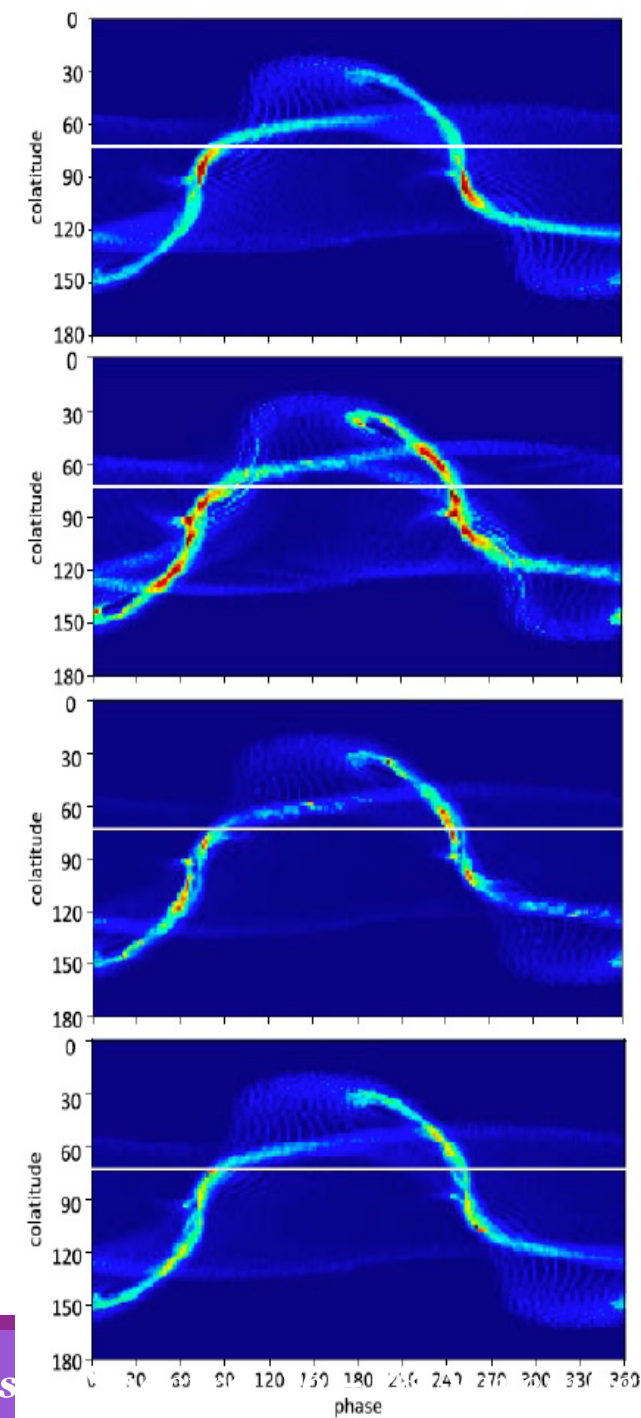
- PL extension of pair spectrum
- Constant pair pitch angle
- Higher number of pairs
- Higher pair SR flux
- SSC from pairs up to 1 TeV matches MAGIC data
- Primary IC up to ~20 TeV
- Photon-photon pair production



# Results: Crab LCs

- Gamma-ray and radio / optical peaks are phase-aligned
- Both gamma peaks survive up to highest energies
- High-altitude emission region near / in CS
- Slow P1/P2 evolution

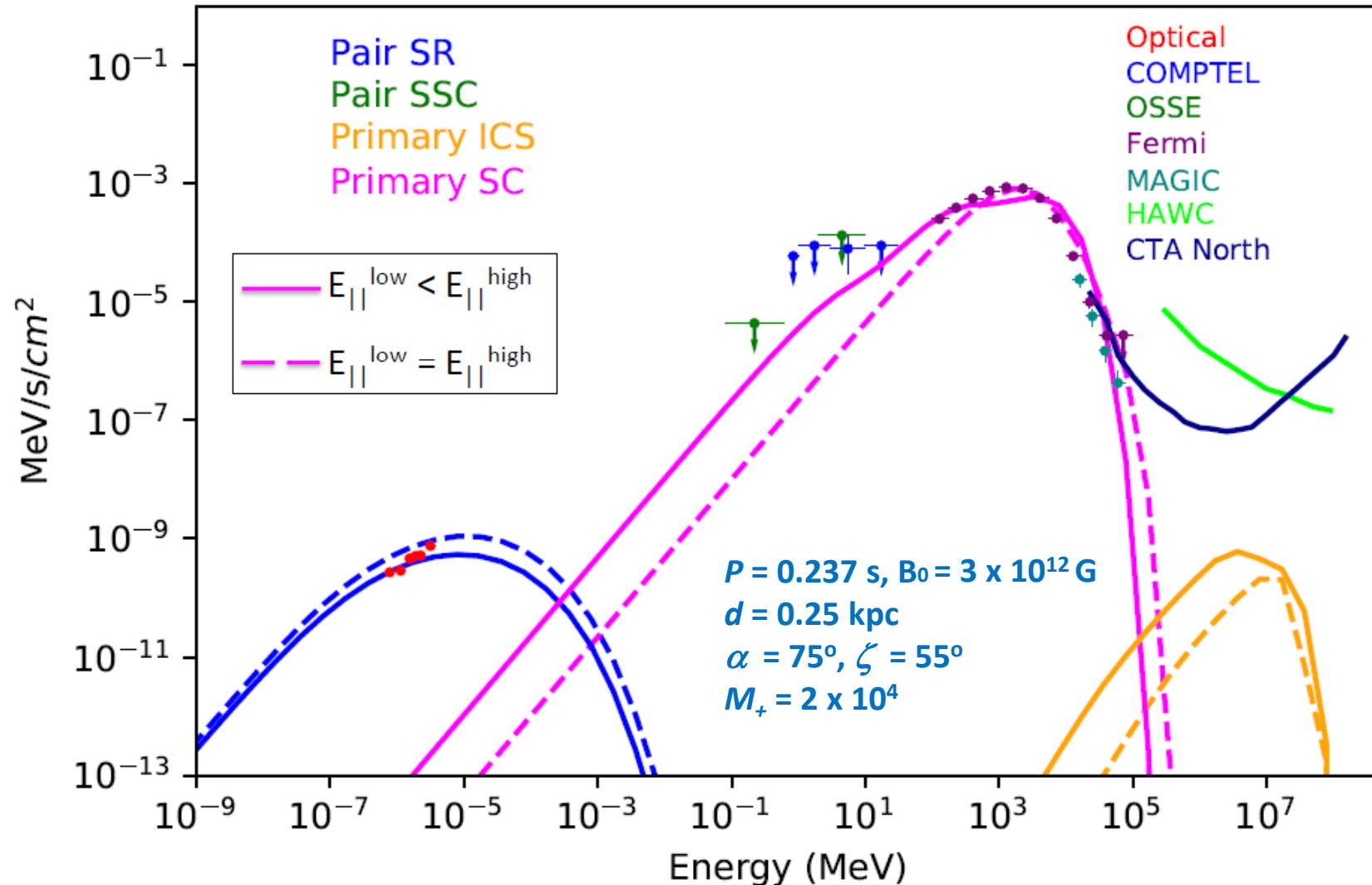
Harding et al. (2021)



# Results: Geminga Spectrum

Harding et al. (2021)

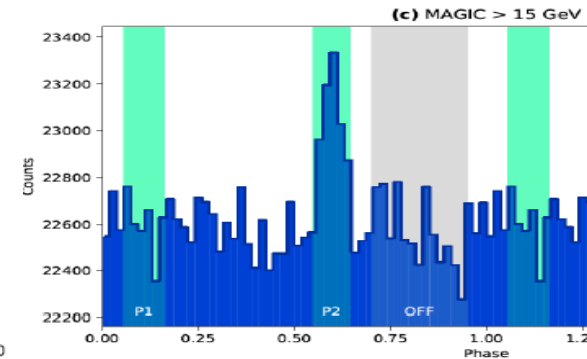
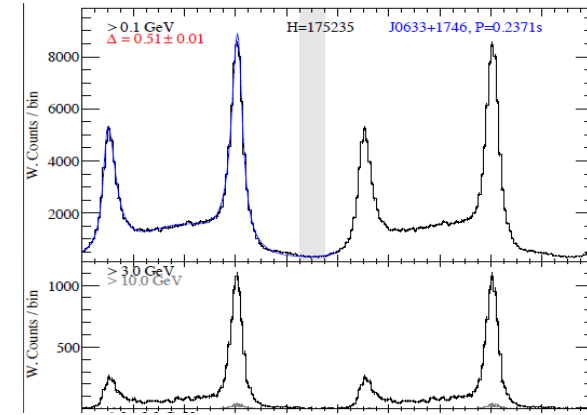
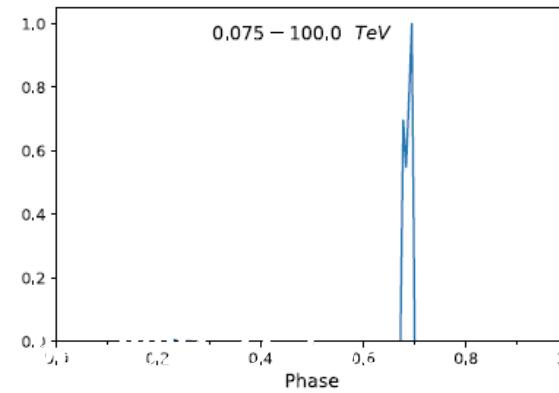
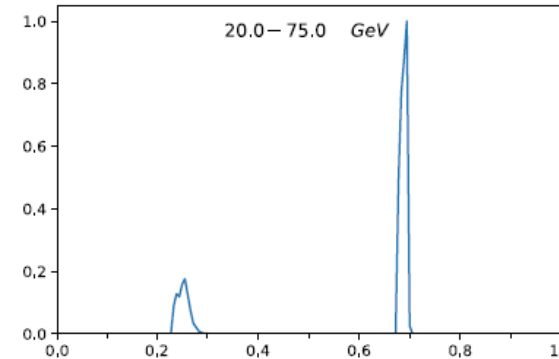
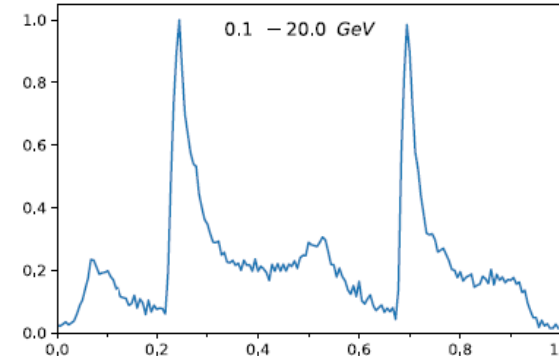
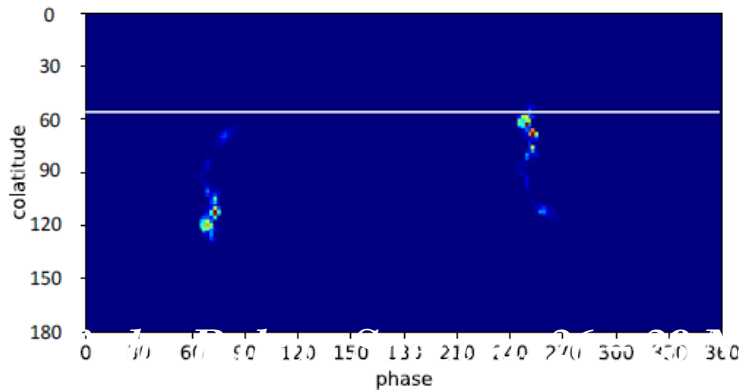
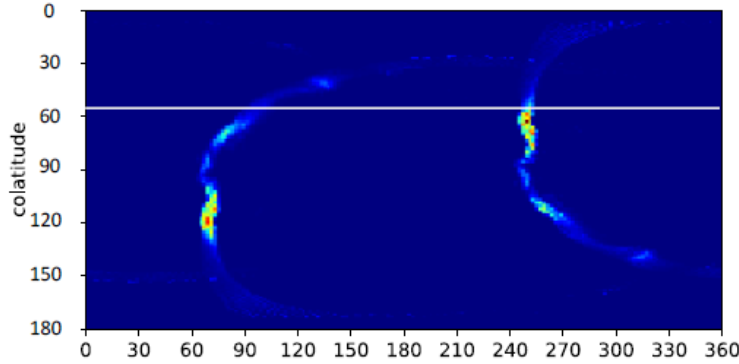
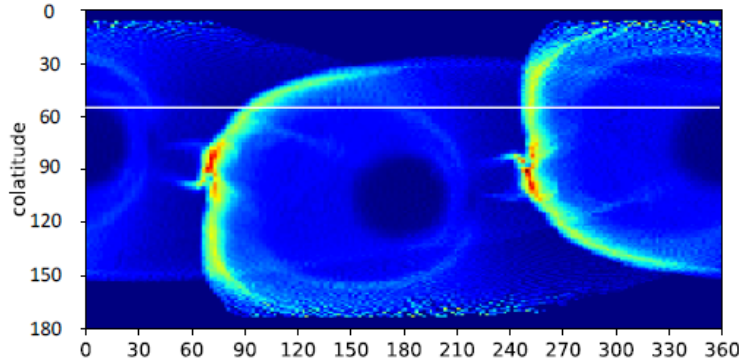
- Assuming a radio flux of 1000 mJy
- Leads to pair SR that can account for UV data
- $E$ -field assumption impacts primary SC spectrum
- Larger  $P$ , larger  $R_{LC}$
- Low pair SR flux (compared to Vela) leads to low IC flux prediction
- MAGIC detection: primary SC





# Results: Geminga LCs

- P1 disappears with energy
- Observed peak width reduction not as pronounced as predicted by the model

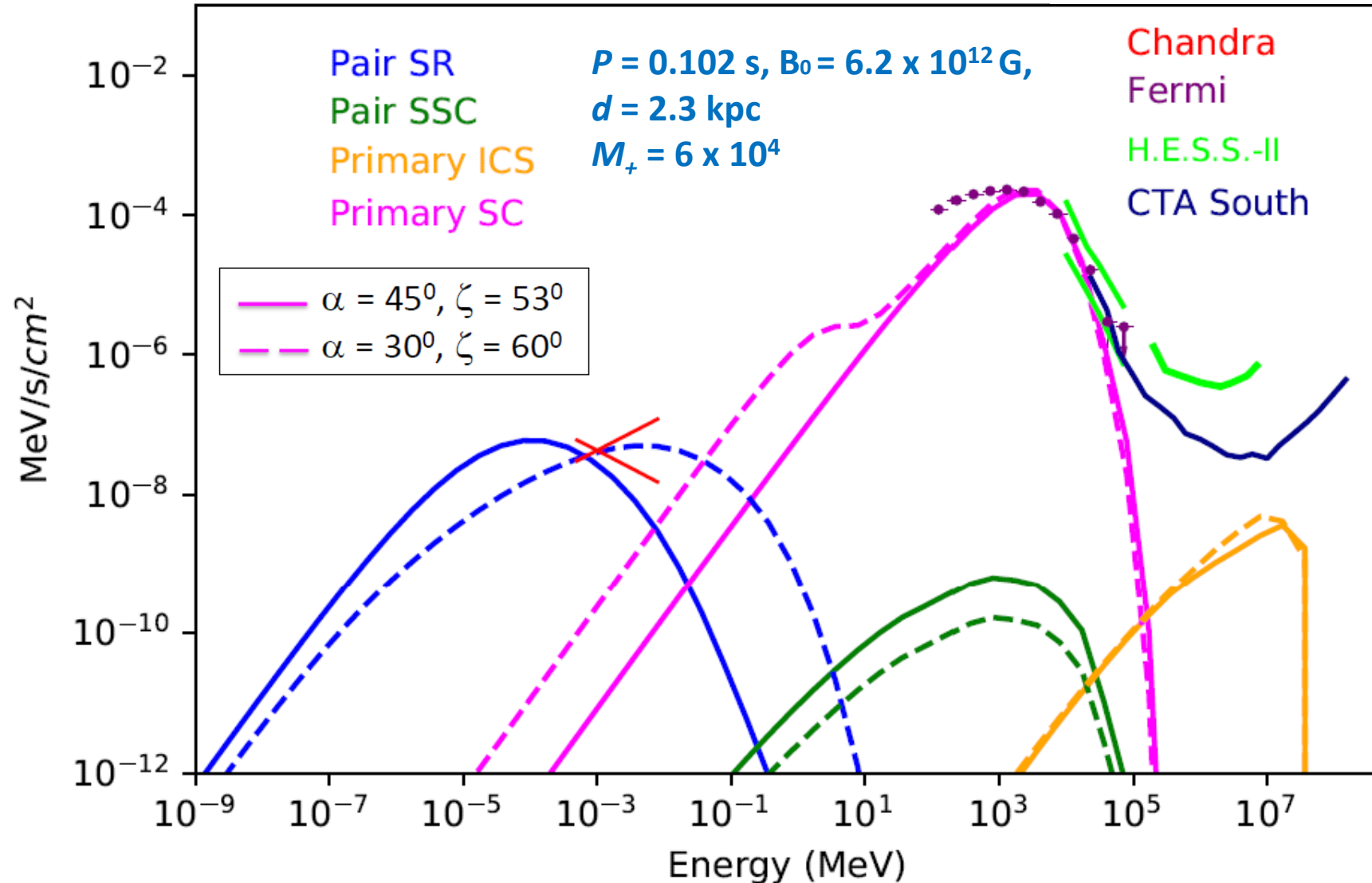
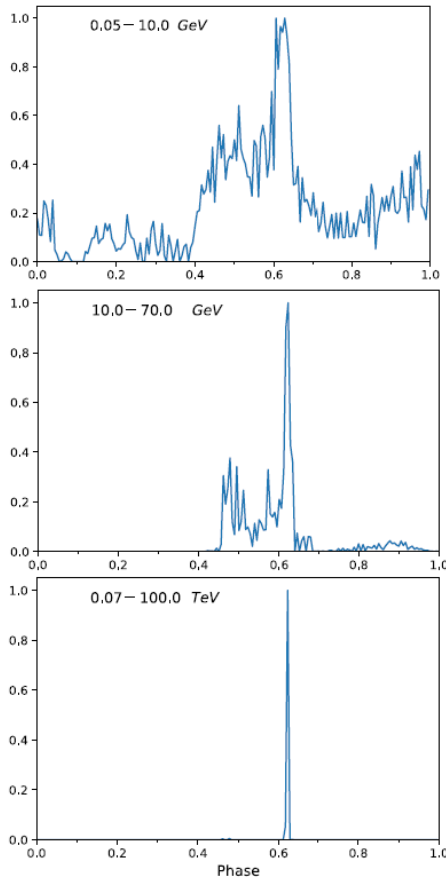


Harding et al. (2021)

# Results: B1706-44

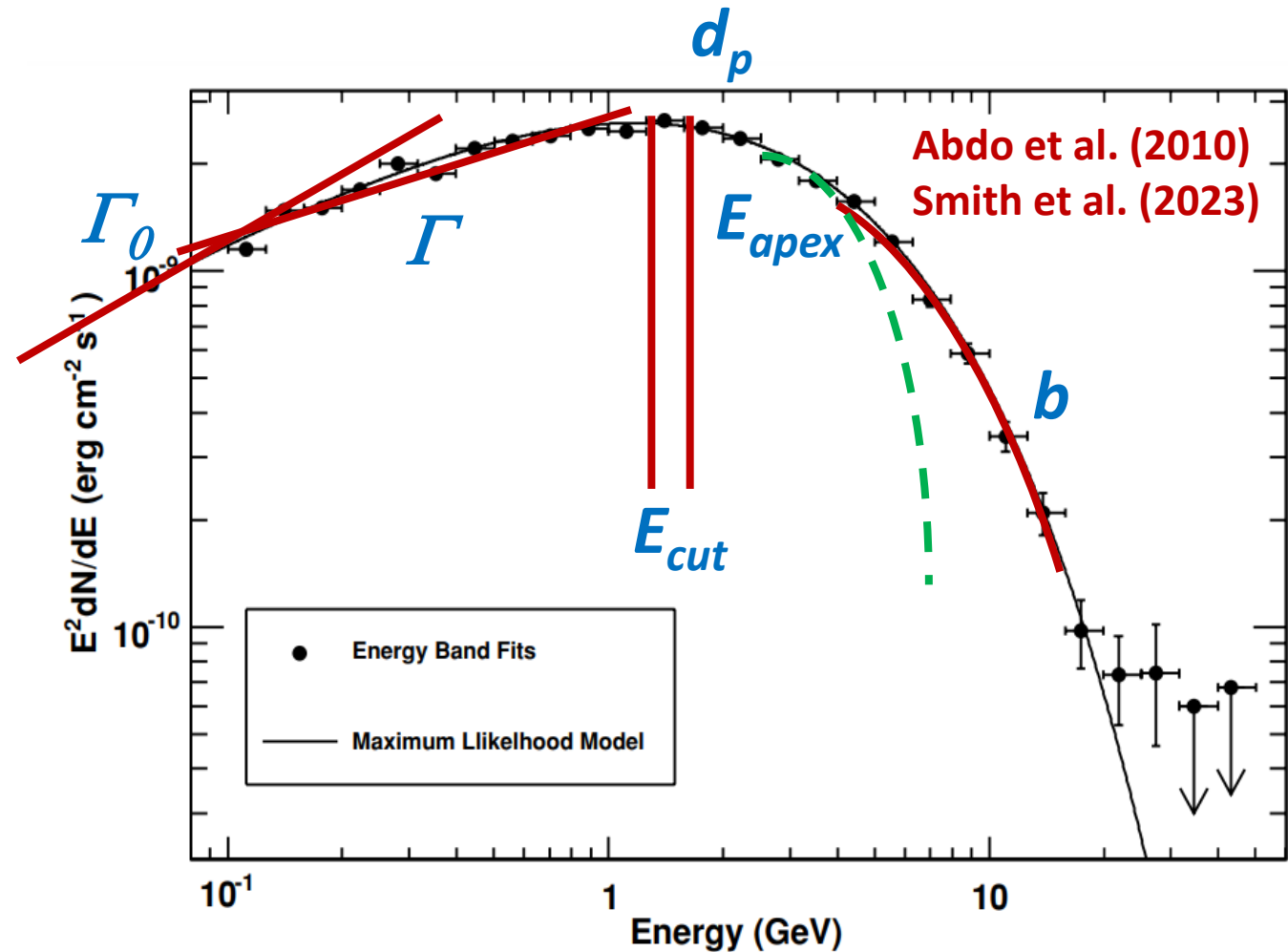
Harding et al. (2021)

- Lower radio luminosity
- Lower pair SR
- Lower primary IC
- H.E.S.S. data: primary SC



# Criticisms / Questions?

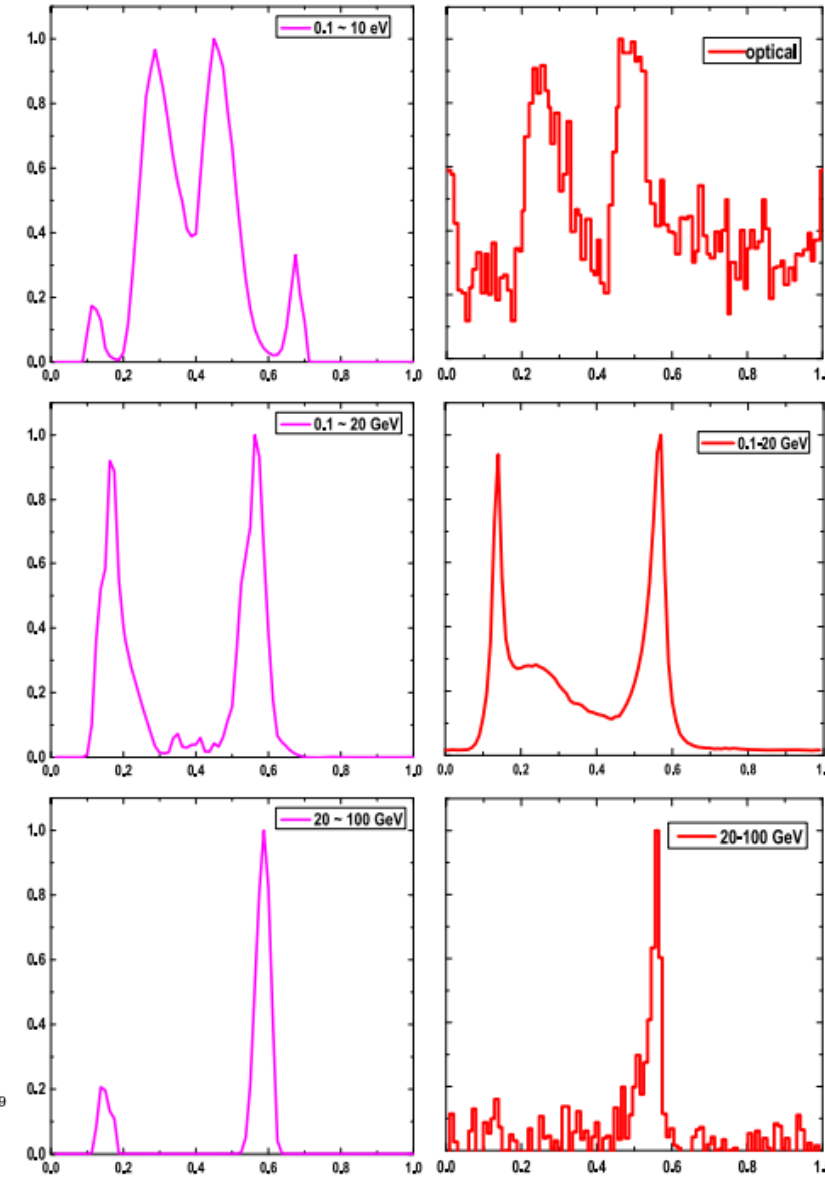
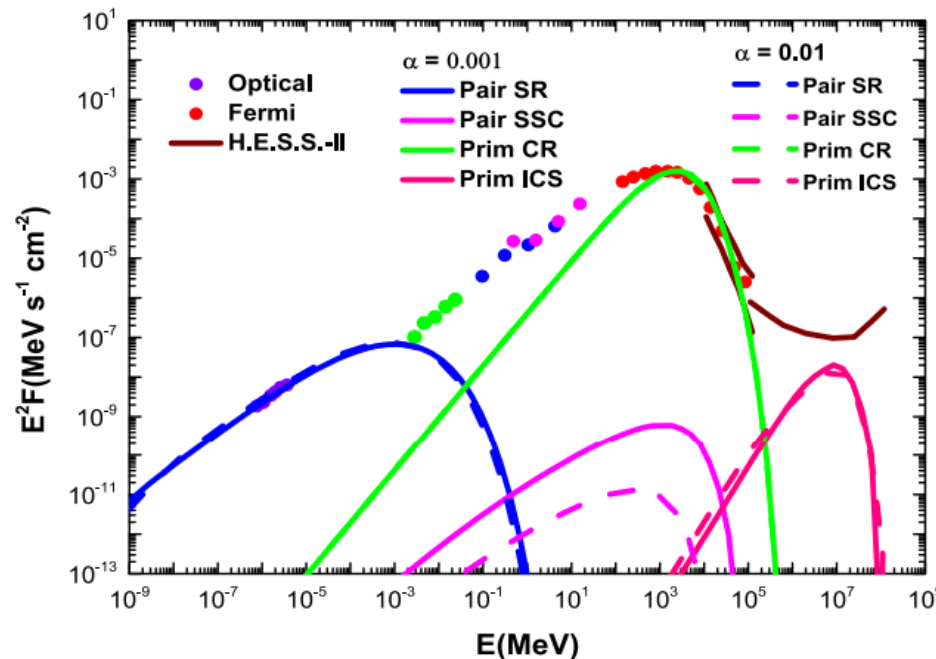
- High  $\gamma$  implied. Which framework?  
Cf. talks by Djannati-Ataï, Philippov, Cerutti, etc.
- Shape of GeV tail: exponential, sub-exponential, PL?
- Do smooth particle trajectories exist in CS? What is the effective  $\rho_c$  in the CS?
- Nature of target photons?
- Acceleration? Energetics?
- Particle injection?



# Improvements?

- Radially and azimuthally-dependent  $E$ -field; pitch angle  $\alpha$  evolution
- Use light curves+spectra [phase-resolved spectroscopy] and polarisation to constrain location of acceleration / emission site(s)
- Study different particle injection / pair cascade scenarios
- Offset dipoles?
- Model discriminants?
- More than one particle population?

Yang & Cao (2024)



# Conclusions

- 20 TeV pulsations from the Vela pulsar! New discoveries being made
- Convolution of particle dynamics & geometry: imprints on **light curves, spectra, polarisation**
- Unprecedented constraints on models:
  - Energetics and emission mechanisms
  - Emission location: In CS [Large  $\rho_c$ ; nature of acceleration?]
  - Field structure via  $\rho_c$ ; P1/P2 vs  $E_\gamma$  effect; *NICER* hotspots
  - Soft photons: Emissivity profiles and spectra of UV / optical
  - Break SC degeneracies:  $E$ -field strength vs  $\rho_c$
- Ongoing observations by current IACTs; CTA Pulsar Programme!

Cf. talk by Djannati-Ataï, Zanin, etc.

# Thanks!



This work is based on the research supported wholly/in part by the National Research Foundation (NRF) of South Africa (grant number 99072). The grant holder acknowledges that opinions, findings, and conclusions or recommendations expressed in any publication generated by the NRF supported research is that of the author(s), and that the NRF accepts no liability whatsoever in this regard.



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*God is higher than anything and anyone, outshining everything you can see in the skies. Who can compare with God, our God, so majestically enthroned, surveying His magnificent heavens and earth? (Psalm 113:4-6 MSG).*